

THE EFFECT OF EARTHQUAKES ON REINFORCED CONCRETE  
BUILDING DESIGN

for

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by

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## THE EFFECT OF EARTHQUAKES ON REINFORCED CONCRETE BUILDING DESIGN

The building under consideration was the Pasadena Furniture Building, on East Colorado St., Pasadena, California. It is a modern reinforced concrete building that may be classed as a warehouse of flat-slab construction.

Instead of checking up over the entire building, one wall column and one interior column of one row of columns was taken as an example of the existing design, and calculations made on these, from the roof to the basement. It was thought that this would be a fair assumption, for the building is essentially a warehouse with regular column spacing.

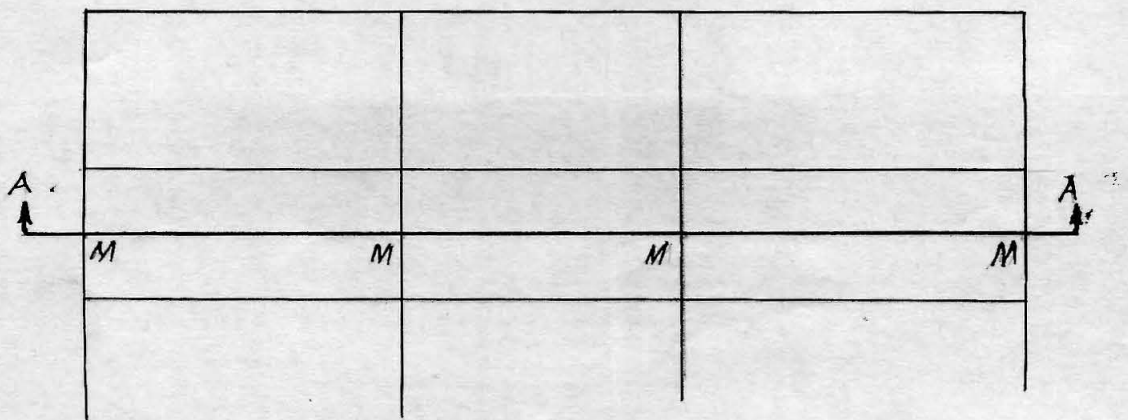
In place of the forces that would result from earthquakes, a horizontal force of ten percent of the dead weight of the building was used. This was thought to be conservative, because the earthquakes are not always of the same magnitude. The average quake has an acceleration of from two to

six feet per second per second. Computing the acceleration that would result from a force of ten percent of the dead weight, it would be

$$F = \frac{m a}{g}, \text{ or } a = \frac{F g}{m}, = \frac{1}{10} 32.2 = 3.22 \text{ ft. per second per second.}$$

This is seen to be a conservative figure. It was found after obtaining the dead weights, that they differed very little from each other on each floor (roof excepted). So an even figure was used to simplify calculations, 20,000 lbs. for each floor and 40,000 lbs. for the roof.

The forces were assumed to act similarly to wind forces. That is, one tenth of the dead weight above one floor was assumed to be the shear on the center of the column directly below that floor. The stresses and moments were found by the Portal Method. The assumption (1) is made that the moment



in the columns is zero at the point M. Also (2) the horizontal shear in any plane A-A is divided by the number of aisles, therefore the outer columns take one-half the shear of an interior column. In this method of computing stresses, the difference in cross-section of the columns does not affect the result. A diagram of the bending moments and direct stresses in the various members for columns 7, 18, 29, and 39, will be found on page 23 and for the plane of columns passing north and south through column 18, on page 48.

The roof beams and girders were checked and found to be sufficiently strong for bending. The required size of flat slab for the bending moment caused by earthquakes was found to be 28.2" deep. Such a depth would be out of the question. It was therefore necessary to change the style of floor construction from flat slab to beam and girder construction.

This was one of the most important results brought out by the investigation. This means that if reinforced concrete buildings are to be designed



to withstand earthquake stresses, it means that it would be necessary to design for beams and girders. This would mean deeper head room than for the flat slab construction as designed, neglecting horizontal forces, but as flat slab construction, considering horizontal forces is out of the question, it is the only way out.

A typical design of the floor system neglecting horizontal forces is given on page 29. It was assumed that the live load of 125 pounds per square foot as not acting, for this would put an unnecessary burden on the members. The bending moment caused by dead weight was added to that caused by the horizontal forces. The negative bending moment caused by the dead weight could have been calculated so as to neutralize an equal amount of positive moment, but this was considered to be negligible.

The shear at the center of the columns is the greatest and the shear at the interior columns is twice as much as that on the wall columns. As the columns are, (with hooping) they are strong

enough to stand the shear. The longitudinal steel will almost be sufficient to stand the bending moment and the direct stress. The method followed in finding the direct stresses gave values for all columns, but the direct stress on the interior columns are neutralized because of the difference in direction of the forces.

All columns are square, that is the core is circular with two inches of concrete outside of each end of a diameter, this makes the side of the square column four inches greater than the core diameter. In calculating for the necessary steel, "d" will be taken as equal to the core diameter plus two inches, "b" equal to one side of the column. Taking into account a reversal of stress, it necessary to have the same amount of steel on opposite sides of the column. The bending moments is twice as much on the interior columns as it is on the wall columns.

The above calculations were made also with horizontal forces acting north and south directions,

as far as they affect columns 7 and 18. No change will be made in the columns to stand the direct stress, for the forces can only act either north and south or east and west. It will be necessary however, to add steel on the north and south sides of the columns to stand the bending stresses.

The amount of stress that the steel that was originally in the columns would stand was considered and applied to that necessary to stand the bending moment. The amount of stress that was in excess of that which the original steel would stand was assumed to act at 16,000 pounds per square inch and the extra steel placed at that point. With the forces acting east and west extra steel was needed on all floors for column 18 and on floors 8, 7, 6, and 5, for column 7. For the north and south forces steel was needed on all except the first floor and the basement for col 18 and on floors 8, 7, 6, and 5, for column 7.

In the calculation of the steel needed in all beams and girders steel is needed both in the top and bottom of the members. Only half of the



steel was carried to the one quarter point on each beam and girder. As very little steel was needed to be added to each column, excepting columns on the 7th, and 8th floors, the extra steel was only extended to the quarter point on each side of the floors, excepting on floors 8, 7, and the basement. The volume of concrete in the columns was assumed to be the same in the old and new design.

The final results show that there is very little difference in the amount of concrete in both designs, but the amount of steel needed in the new design is more than twice as great as in the old design.

There is the question that if the original building had been of beam and girder design, whether there would have been as much difference in the amount of steel needed. Off hand it seems that the amount of steel needed would be about one and one half times as much, as when neglecting the horizontal forces.



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# Dead Weight of Members (Col 7, 18, 29, 39)

## Roof Dead Load

### Column #7

$$L.L. = \left( \frac{18' + 19'}{2} \right) \times \frac{24.5}{2} \times 30 = 6.798$$

$$D.L. = 39.2 - 6.8 = 32.4 \text{ Kips}$$

### Column #18

$$L.L. = \left( \frac{18 \times 19}{2} \right) \times \frac{24.5}{2} \times 30 = 13.596$$

$$D.L. = 61.2 - 13.6 = 47.6 \text{ Kips}$$

### Column #29

$$L.L. = 13.6$$

$$D.L. = 169.7 - 13.6 = 156.1 \text{ Kips}$$

### Column #39

$$L.L. = 6.798$$

$$D.L. = 168.3 - 6.8 = 161.5 \text{ Kips}$$

## Total D.L. on Roof

$$32.4 + 47.6 + 156.1 + 161.5 = 397.6 \text{ Kips}$$

Column	#7	#18	#29	#39
Column Dimensions	16X16	16X16	20X20	20X20

$$D.L. \text{ of Roof} = 397.6 \text{ Kips}$$



2

8th floor. Column #7

$$L.L. = \left( \frac{18+19}{2} \right) \frac{24.5}{2} \times 155 = 35.126$$

$$D.L. = 121.1 - 35.1 = 86.0 \text{ Kips}$$

Column #18

$$L.L. = 70.2$$

$$D.L. = 176.7 - 70.2 = 106.5 \text{ kips}$$

Column #29

$$L.L. = 70.2$$

$$D.L. = 281.7 - 70.2 = 211.5 \text{ Kips}$$

Column #39

$$L.L. = 35.1$$

$$D.L. = 239.7 - 35.1 = 204.6 \text{ kips}$$

Total

$$86.0 + 106.5 + 211.5 + 204.6 = 608.6 \text{ Kips}$$

Column	#7	#18	#29	#39
Column Dimensions	18X18	20X20	24X24	23X23

D.L. of 8th floor

$$608.6 - 397.6 = 211.0 \text{ Kips}$$



7th floor

## Column #7

$$LL = 226.25 \times (153 + 125) = 63.455$$

$$DL = 201.5 - 63.5 = 138.0$$

## Column #18

$$LL = 126.8$$

$$DL = 289.7 - 126.8 = 162.9$$

## Column #29

$$LL = 126.8$$

$$DL = 389.7 - 126.8 = 262.9$$

## Column #39

$$LL = 63.5$$

$$DL = 310.0 - 63.5 = 246.5$$

## Total

$$138.0 + 162.9 + 262.9 + 246.5 = 810.3 \text{ Kips}$$

	7	18	29	39
Dimensions	22x22	24x24	27x27	25x25

## DL of 7th floor

$$810.3 - 608.6 = 201.7 \text{ Kips}$$

6th floor

Column #7

$$LL = 226.625 \times (280 + 125) = 917.83$$

$$DL = 280.1 - 91.9 = 188.2$$

Column #18

$$LL = 183.8$$

$$DL = 394.2 - 183.8 = 210.4$$

Column #29

$$LL = 183.8$$

$$DL = 493.7 - 183.8 = 309.9$$

Column #39

$$LL = 91.9$$

$$DL = 378.8 - 91.9 = 276.9$$

Total

$$188.2 + 210.4 + 309.9 + 276.9 = 985.4 \text{ Kips}$$

	7	18	29	39
Dimensions	24x24	27x27	28x28	27x27

D.L. of 6th floor

$$985.4 - 810.3 = 175.1 \text{ Kips}$$

5th floor

Column #7

$$LL = 226.625(405 + 125) = 120.111$$

$$DL = 361.0 - 120.1 = 240.9$$

Column #18

$$LL = 240.2$$

$$DL = 504.7 - 240.2 = 264.5$$

Column #29

$$LL = 240.2$$

$$DL = 601.2 - 240.2 = 361.0$$

Column #39

$$LL = 120.1$$

$$DL = 450.8 - 120.1 = 330.7$$

Total

$$240.9 + 264.5 + 361.0 + 330.7 = 1197.1$$

---

7	18	29	39
26x26	28x28	30x30	29x29

D.L. of 5th floor

$$1197.1 - 985.4 = 211.7 \text{ Kips.}$$



4th floor  
Column #1

$$LL = 226.625(530+125) = 148,439$$

$$DL = 440.2 - 148.4 = 291.8$$

Column #18

$$LL = 296.8$$

$$DL = 611.9 - 296.8 = 315.1$$

Column #29

$$LL = 296.8$$

$$DL = 705.0 - 296.8 = 408.2$$

Column #39

$$LL = 148.4$$

$$DL = 521.0 - 148.4 = 372.6$$

Total

$$291.8 + 315.1 + 408.2 + 372.6 = 1387.7 \text{ Kips.}$$

---

7	18	29	39
28x28	30x30	32x32	30x30

D.L. on 4th floor

$$1387.7 - 1197.1 = 190.6 \text{ Kips}$$



3rd floor

Column #7

$$LL = 226.625(605 + 125) = 176.767$$

$$DL = 518.1 - 176.8 = 341.3$$

Column #18

$$LL = 353.6$$

$$DL = 718.0 - 353.6 = 354.4$$

Column #29

$$LL = 353.6$$

$$DL = 809.0 - 353.6 = 445.4$$

Column #39

$$LL = 176.8$$

$$DL = 592.0 - 176.8 = 415.2$$

Total

$$341.3 + 354.4 + 445.4 + 415.2 = 1556.3$$

7	18	29	39
30x30	32x32	34x34	34x34

D.L. on 3rd floor

$$1556.3 - 1387.7 = 168.6 \text{ Kips}$$

2nd floor  
Column # 7

$$LL = 226.25(780 + 125) = 205,096$$

$$DL = 594.6 - 205.1 = 389.5$$

Column #18

$$LL = 410.2$$

$$DL = 825.3 - 410.2 = 415.1$$

Column #29

$$LL = 410.2$$

$$DL = 914.0 - 410.2 = 503.8$$

Column #39

$$LL = 205.1$$

$$DL = 664.0 - 205.1 = 458.9$$

Total

$$389.5 + 415.1 + 503.8 + 458.9 = 1767.3$$

7	18	29	39
31X31	34X34	34X34	33X33

D.L. on 2nd floor

$$1767.3 - 1556.3 = 2110 \text{ Kips.}$$

1st floor

Column #7

$$LL = 226.625(905 + 125) = 233,424$$

$$DL = 6754 - 233.4 = 442.0$$

Column #18

$$LL = 466.8$$

$$DL = 935.3 - 466.8 = 468.5$$

Column #29

$$LL = 466.8$$

$$DL = 1023.0 - 466.8 = 556.2$$

Column #39

$$LL = 233.4$$

$$DL = 740 - 233.4 = 506.6$$

Total

$$442.0 + 468.5 + 556.2 + 506.6 = 1973.3 \text{ Kips.}$$

>  
33x33

18  
34x34

29  
36x36

39  
34x34

D.L. on 1st floor

$$1973.3 - 1767.3 = 206.0 \text{ Kips.}$$



Stresses & Moments to be found by Portal Method.

Horizontal shear in any plane is divided by number of aisles.

∴ An outer column takes but half the shear of an interior column.

In this method of computing stresses the difference in cross-section of the columns does not effect results.

Direct stress in columns

8th floor (Any aisle)

$$\frac{40 \times 14.33}{3} \div \frac{73}{2} = 3.92$$

direct stresses coming on interior columns from the adjacent aisles are equal in amount but opposite in direction. Therefore their algebraic sum is zero

7th floor

$$\left[ 40 \left( 14.33 + \frac{11.75}{2} \right) + 20 \left( \frac{11.75}{2} \right) \right] \div 73 = 12.65$$

6th floor

$$\left[ 40 \left( 14.33 + 11.75 + \frac{11.75}{2} \right) + 20 \left( 11.75 + \frac{11.75}{2} \right) + 20 \left( \frac{11.75}{2} \right) \right] \div 73 = 23.95$$

5th floor

$$\left[ 40 \left( 14.33 + 2 \times 11.75 + \frac{11.75}{2} \right) + 20 \left( 2 \times 11.75 + \frac{11.75}{2} \right) + 20 \left( 11.75 + \frac{11.75}{2} \right) + 20 \left( \frac{11.75}{2} \right) \right] \div 73 = 38.49$$



#### 4th floor

$$[40(14.33 + 3.5 \times 11.75) + 20(3.5 \times 11.75) + 20(2.5 \times 11.75) + 20(1.5 \times 11.75) + 20(.5 \times 11.75)] \div 73 = 56.2$$

#### 3rd floor

$$[40(14.33 + 4.5 \times 11.75) + 20(4.5 \times 11.75) + 20(3.5 \times 11.75) + 20(2.5 \times 11.75) + 20(1.5 \times 11.75) + 20(.5 \times 11.75)] \div 73 = 72.2$$

#### 2nd floor

$$[40(14.33 + 5.5 \times 11.75) + 20(5.5 \times 11.75) + 20(4.5 \times 11.75) + 20(3.5 \times 11.75) + 20(2.5 \times 11.75) + 20(1.5 \times 11.75) + 20(.5 \times 11.75)] \div 73 = 101.0$$

#### 1st floor

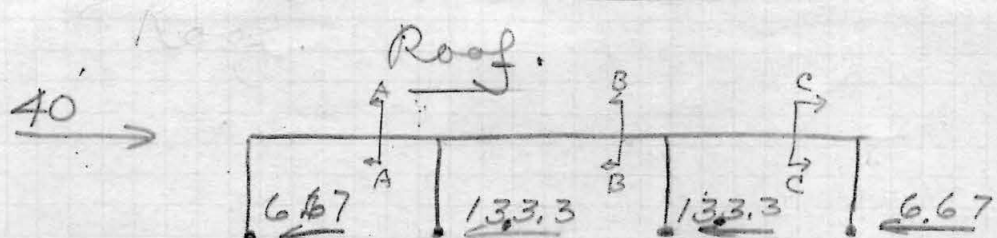
$$[40(14.33 + 6 \times 11.75 + .5 \times 12.75) + 20(6 \times 11.75 + .5 \times 12.75) + 20(5 \times 11.75 + .5 \times 12.75) + 20(4 \times 11.75 + .5 \times 12.75) + 20(3 \times 11.75 + 1.5 \times 12.75) + 20(2 \times 11.75 + 1.5 \times 12.75) + 20(1 \times 11.75 + 1.5 \times 12.75) + 20(.5 \times 12.75)] \div 73 = 129.6$$

#### Basement

$$[40(14.33 + 6 \times 11.75 + 1.5 \times 12.75) + 20(6 \times 11.75 + 1.5 \times 12.75) + 20(5 \times 11.75 + 1.5 \times 12.75) + 20(4 \times 11.75 + 1.5 \times 12.75) + 20(3 \times 11.75 + 1.5 \times 12.75) + 20(2 \times 11.75 + 1.5 \times 12.75) + 20(1 \times 11.75 + 1.5 \times 12.75) + 20(1.5 \times 12.75)] \div 73 = 162.7$$

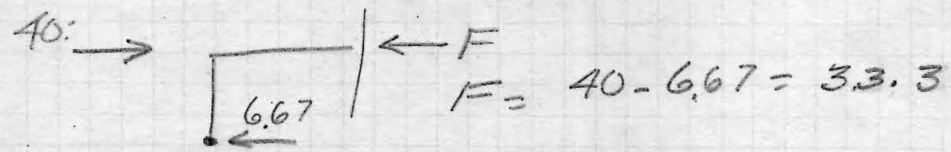
# Direct Stresses in Beams

12

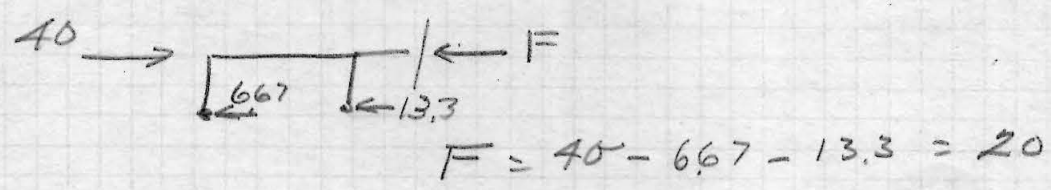


all circles take equal shears.

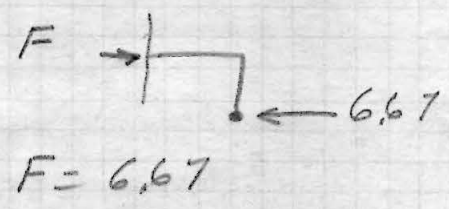
## Section AA



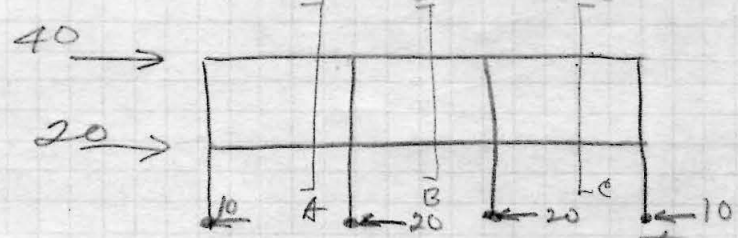
## Section B-B



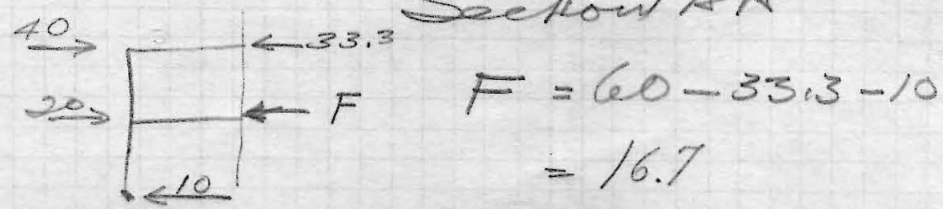
## section C-C

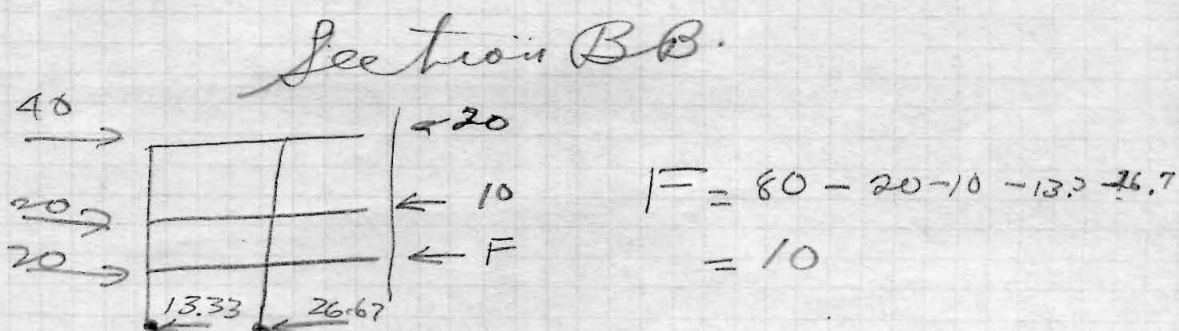
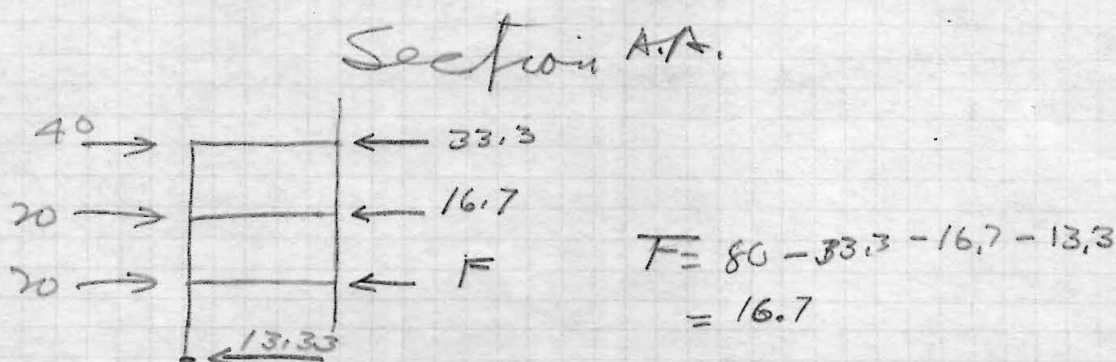
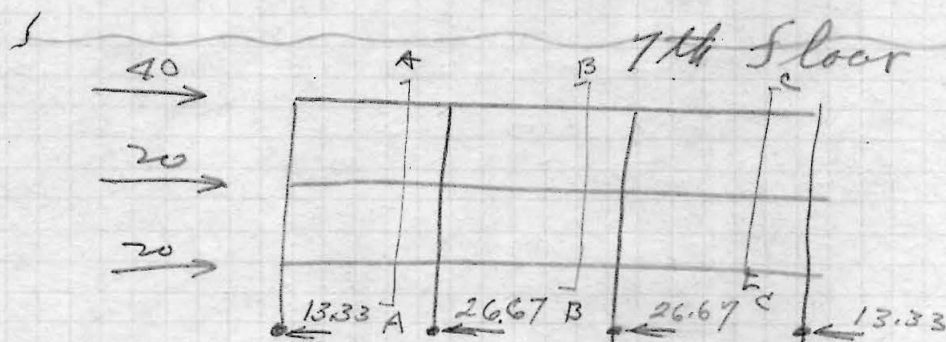
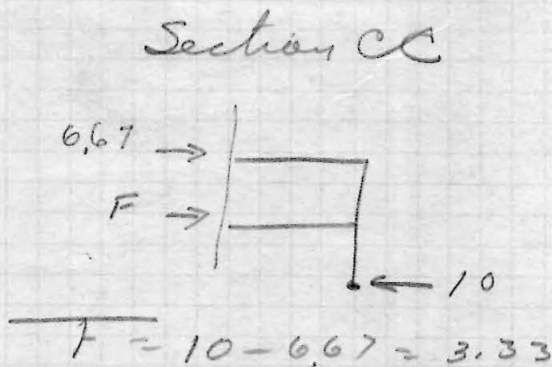
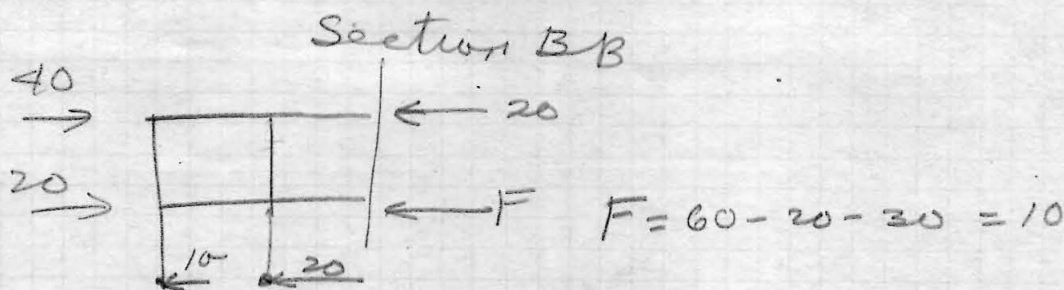


## 8th floor

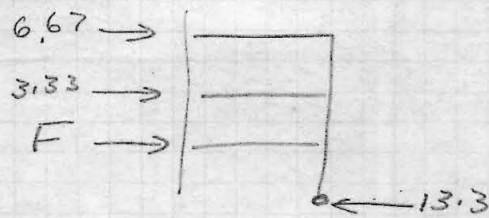


## Section AA









$$F = 13.3 - 6.67 - 3.33$$

$$= 3.33$$

These stresses will be the same in all girders of the remaining floors, that is in floors 6, 5, 4, 3, 2, 1 for sections A-A corresponding to those used in above illustrations, the stresses will be 6.7, section B-B = 10, section C-C = 3.33

# Bending Moments in Girders

Roof.



$$M_1 = 6.67 \times \frac{14.33}{2} = +47.6 \text{ ft-lbs.}$$

$$M_2 = 6.67 \times \frac{14.33}{2} - 39.2 \times 24.33 = -47.8$$

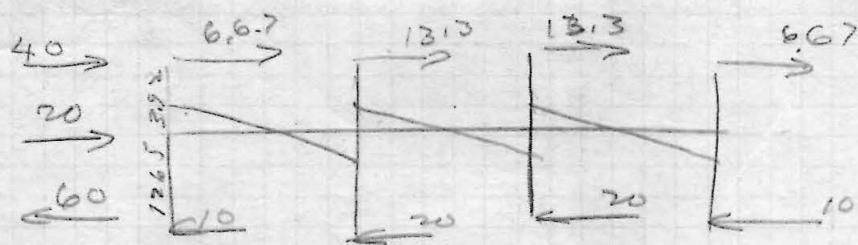
$$M_3 = (6.67 + 13.33) \frac{14.33}{2} - 39.2 \times 24.33 = +47.9$$

$$M_4 = (6.67 + 13.33) \frac{14.33}{2} - 39.2 \times 48.66 = -47.5$$

$$M_5 = (6.67 + 13.33 + 13.33) \frac{14.33}{2} - 39.2 \times 48.66 = +48.2$$

$$M_6 = (6.67 + 13.33 + 13.33) \frac{14.33}{2} - 39.2 \times 73 = -47.2$$

# 8th Floor



$$M_1 = 6.67 \times \frac{14.33}{2} + 10 \times \frac{11.75}{2} = +106$$

$$M_2 = 6.67 \times \frac{14.33}{2} + 10 \times \frac{11.75}{2} - (12.65 - 39.2) \times 24.33 = -106$$

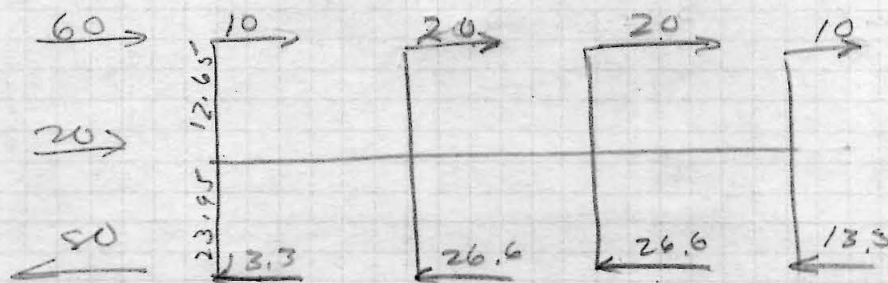
$$M_3 = (6.67 + 13.3) \times \frac{14.33}{2} + (10 + 20) \times \frac{11.75}{2} - (12.65 - 39.2) \times 24.33 = +106$$

$$M_4 = (6.67 + 13.3) \times \frac{14.33}{2} + (10 + 20) \times \frac{11.75}{2} - (12.65 - 39.2) \times 48.66 = -106$$

$$M_5 = (6.67 + 13.3 + 13.3) \times \frac{14.33}{2} + (10 + 20 + 20) \times \frac{11.75}{2} - (12.65 - 39.2) \times 48.66 = +106$$

$$M_6 = (6.67 + 13.3 + 13.3) \times \frac{14.33}{2} + (10 + 20 + 20) \times \frac{11.75}{2} - (12.65 - 39.2) \times 73 = -106$$

# 7th Floor



$$M_1 = (10 + 13.3) \times \frac{11.75}{2} = +137.0$$

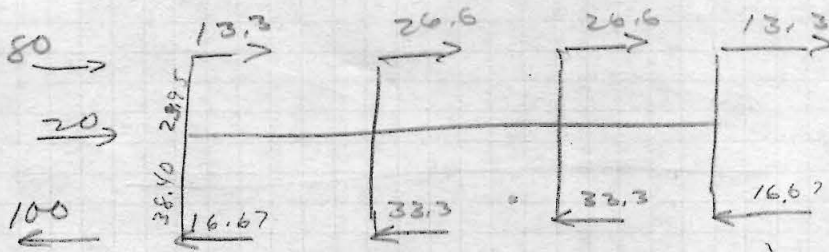
$$M_2 = (10 + 13.3) \times \frac{11.75}{2} - (23.95 - 12.65) \times 24.33 = -138$$

$$M_3 = (10 + 13.3 + 20 + 26.6) \times \frac{11.75}{2} - (23.95 - 12.65) \times 24.33 = -137$$

$$-M_4 = +M_5 = -M_6 = 137$$



## 6th Floor.



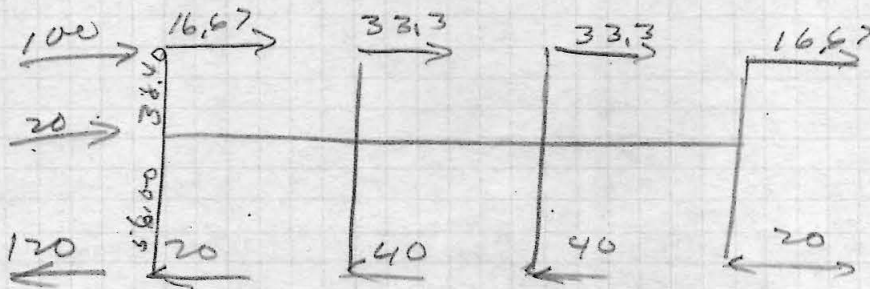
$$M_1 = (13.3 + 16.67) \frac{11.75}{2} = +176.3$$

$$M_2 = (13.3 + 16.67) \frac{11.75}{2} - (38.40 - 23.95) 24.33 = -175.7$$

$$M_3 = (13.3 + 16.67 + 26.6 + 33.3) \frac{11.75}{2} - (38.40 - 23.95) 24.33 = +176.5$$

$$-M_4 = M_5 = -M_6 = 176.5$$

## 5th Floor



$$M_1 = (16.67 + 20) \frac{11.75}{2} = +215.0$$

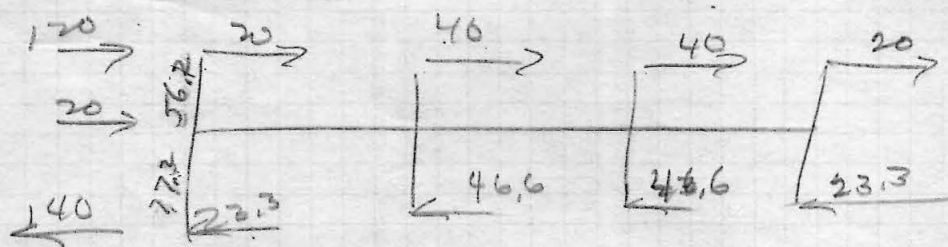
$$M_2 = (16.67 + 20) \frac{11.75}{2} - (56.20 - 38.40) 24.33 = -216$$

$$M_3 = (16.67 + 20 + 33.3 + 40) \frac{11.75}{2} - (56.20 - 38.40) 24.33 = +215$$

$$-M_4 = M_5 = -M_6 = 215$$

# 4th Floor

18



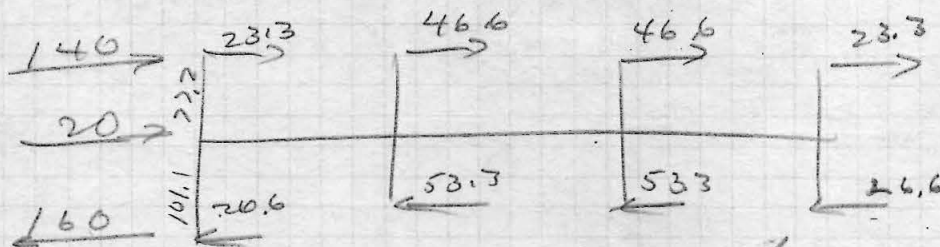
$$M_1 = (20 + 23.3) \frac{11.75}{2} = +254.5$$

$$M_2 = (20 + 23.3) \frac{11.75}{2} - (77.2 - 56.2) 24.33 = -255$$

$$M_3 = (20 + 23.3 + 40 + 46.6) \frac{11.75}{2} - (77.2 - 56.2) 24.33 = +254$$

$$-M_4 = M_5 = -M_6 = 254.5$$

## 3rd Floor



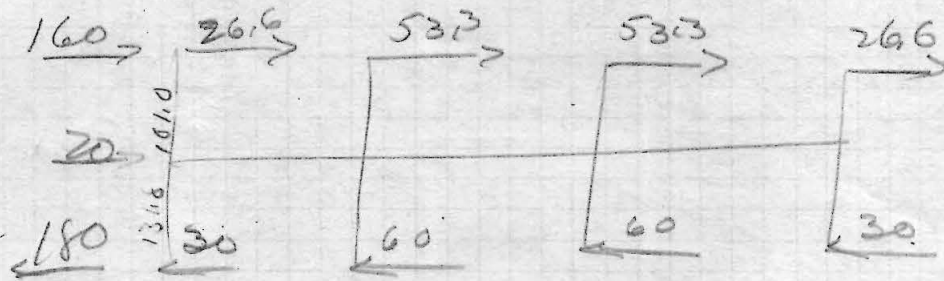
$$M_1 = (23.3 + 26.6) \frac{11.75}{2} = +293.6$$

$$M_2 = (23.3 + 26.6) \frac{11.75}{2} - (101.0 - 77.2) 24.33 = -294.5$$

$$M_3 = (23.3 + 26.6 + 46.6 + 53.3) \frac{11.75}{2} - (101.0 - 77.2) 24.33 = +294$$

$$-M_4 = M_5 = -M_6 = 294.0$$

## 2nd Floor.



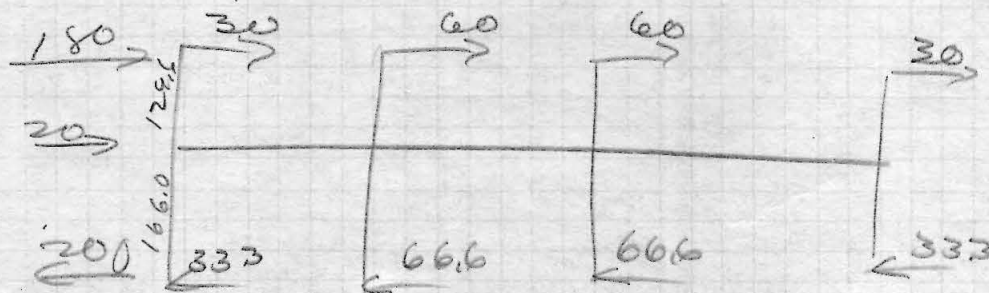
$$M_1 = 26.6 \times \frac{10.10}{2} + 30 \times \frac{10.10}{2} = 347.7$$

$$M_2 = 26.6 \times \frac{10.10}{2} + 30 \times \frac{10.10}{2} - (129.6 - 101.0) \times 24.33 = -347.0$$

$$M_3 = (26.6 + 53.3) \times \frac{10.10}{2} + (30 + 60) \times \frac{10.10}{2} - (129.6 - 101.0) \times 24.33 = +348.0$$

$$-M_4 = M_5 = -M_6 = 347.7$$

## 1st Floor.



$$M_1 = (30 + 33.3) \times \frac{12.95}{2} = +403.0$$

$$M_2 = (30 + 33.3) \times \frac{12.95}{2} - (162.7 - 129.6) \times 24.33 = -402$$

$$M_3 = (30 + 33.3 + 60 + 66.6) \times \frac{12.95}{2} - (162.7 - 129.6) \times 24.33 = 405$$

$$-M_4 = M_5 = -M_6 = 403$$



Roof self story col

$$\text{Outer col.} = 6.67 \times \frac{14.33}{2} = 47.8$$

$$\text{inner col.} = 13.3 \times \frac{14.33}{2} = 95.6$$

} Page 15

8th floor  
8th story col.

$$\text{outer col} = 6.67 \times \frac{14.33}{2} = 47.8$$

$$\text{inner col} = 13.3 \times \frac{14.33}{2} = 95.6$$

7th story col

$$\text{outer col} = 10 \times \frac{11.75}{2} = 58.75$$

$$\text{inner col} = 20 \times \frac{11.75}{2} = 117.5$$

} P. 16

7th Floor

7th story col

$$\text{outer col} = 10 \times \frac{11.75}{2} = 58.75$$

$$\text{inner col} = 20 \times \frac{11.75}{2} = 117.5$$

6th story col

$$\text{outer col} = 13.3 \times \frac{11.75}{2} = 78.3$$

$$\text{inner col} = 26.6 \times \frac{11.75}{2} = 156.6$$

} Page 16.

6th Floor

6th story col.

$$\text{outer col} = 13.3 \times \frac{11.75}{2} = 78.3$$

$$\text{in col} = 26.6 \times \frac{11.75}{2} = 156.6$$

5th story col

$$\text{outer col} = 16.67 \times \frac{11.75}{2} = 98.4$$

$$\text{inner} = 33.33 \times \frac{11.75}{2} = 196.8$$

} P. 17

5th Floor

5th story col

$$\text{outer col} = 16.67 \times \frac{11.75}{2} = 98.4$$

$$\text{inner col} = 33.3 \times \frac{11.75}{2} = 196.8$$

4th story col

$$\text{outer col} = 20 \times \frac{11.75}{2} = 117.5$$

$$\text{inner col} = 40 \times \frac{11.75}{2} = 235.0$$

} Pay 17

4th Floor

4th story col

$$\text{outer col} = 20 \times \frac{11.75}{2} = 117.5$$

$$\text{inner col} = 40 \times \frac{11.75}{2} = 235.0$$

3rd story col

$$\text{outer col} = 23.3 \times \frac{11.75}{2} = 137.0$$

$$\text{inner col} = 46.6 \times \frac{11.75}{2} = 274.0$$

} P. 18

3rd Floor

3rd story col

$$\text{outer col} = 23.3 \times \frac{11.75}{2} = 137.0$$

$$\text{inner col} = 46.6 \times \frac{11.75}{2} = 274.0$$

2nd story col

$$\text{outer col} = 26.6 \times \frac{11.75}{2} = 156.5$$

$$\text{inner col} = 53.3 \times \frac{11.75}{2} = 313.0$$

} P. 18

## 2nd Floor

2nd story col

$$\text{outer col} = 26.6 \times \frac{11.25}{2} = 156.5$$

$$\text{inner col} = 53.2 \times \frac{11.25}{2} = 313.0$$

1st story col

$$\text{outer col} = 30 \times \frac{12.75}{2} = 191.4 \quad \left. \vphantom{\frac{12.75}{2}} \right\} \text{P. 19}$$

$$\text{inner col} = 50 \times \frac{12.75}{2} = 382.8$$

## 1st Floor

$$\text{outer col} = 30 \times \frac{12.75}{2} = 191.4 \quad \left. \vphantom{\frac{12.75}{2}} \right\} \text{1st story col}$$

$$\text{inner col} = 50 \times \frac{12.75}{2} = 382.8$$

basement col

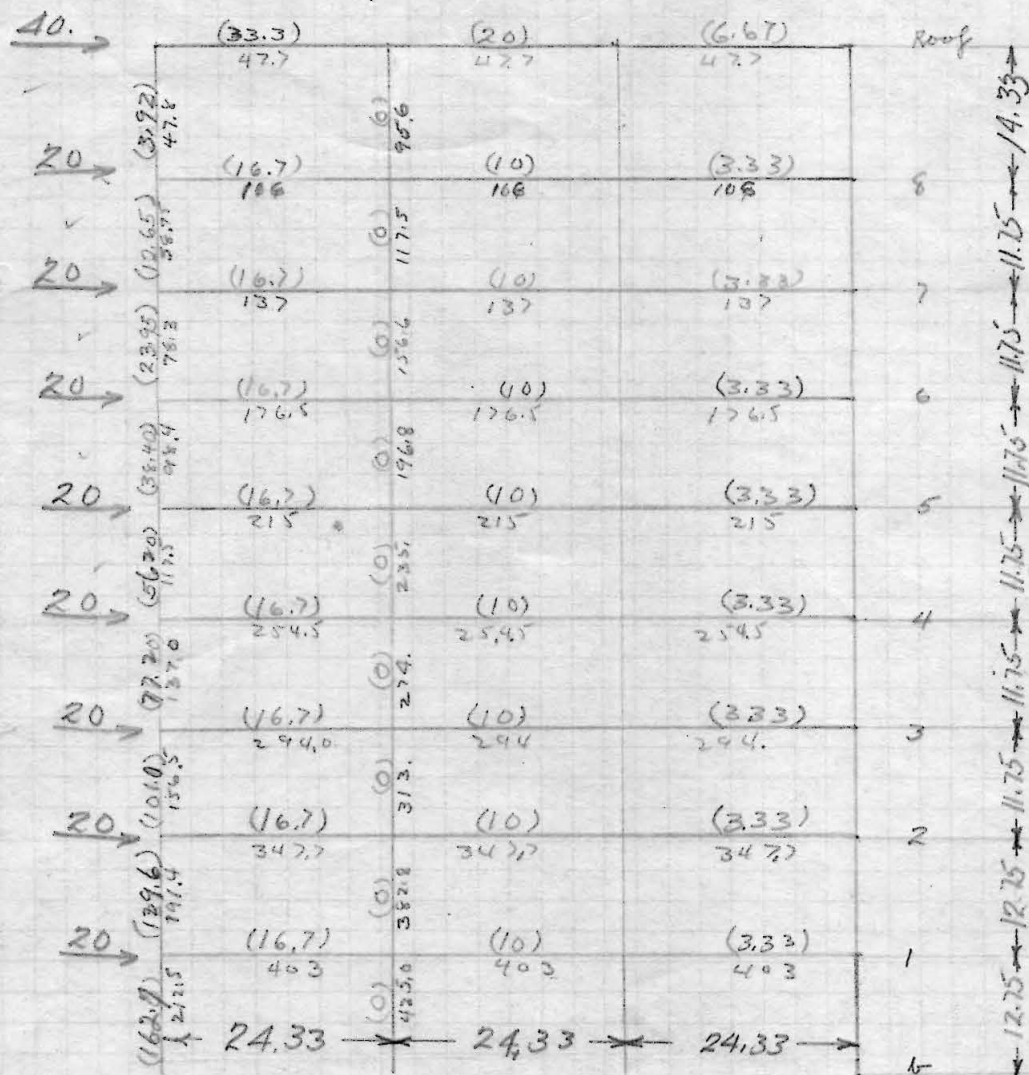
$$\text{outer col} = 33.3 \times \frac{12.75}{2} = 212.5 \quad \left. \vphantom{\frac{12.75}{2}} \right\} \text{P. 19}$$

$$\text{inner col} = 66.6 \times \frac{12.75}{2} = 425.0$$



# Diagram Showing Direct Stresses and B.M.

Columns #7, #18, #29, #39



#7

#18

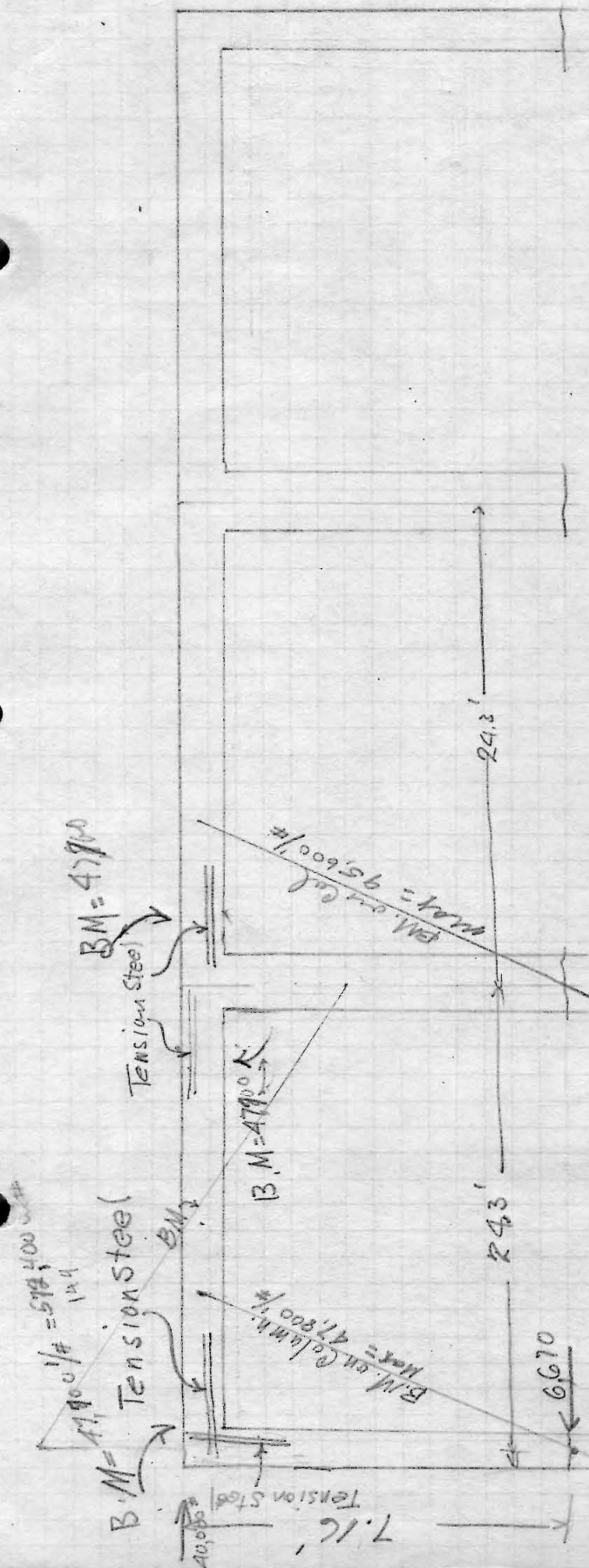
#29

#39

(33.3) = direct stress of 33,300 lbs.  
47.7 = B.M. of 47,700 ft-lbs.

An average of 20 kips is used on floors

40 kips on roof.



Roof Beam End Span 13.23

$$BM = 149,000$$

$$RM = 133.8 \times 12 \times 28 \times 28 = 1,260,000 \text{ in}^4$$

$$a_s = .0077 \times 12 \times 28 = 1.817 \text{ in.}$$

$\therefore$  amt. of steel necessary to carry 149,000 in<sup>4</sup> = 1.817

but 4-1 $\frac{1}{8}$ " bars or 5.06 sq in were used.

The beam will stand 1,260,000 in<sup>4</sup> ( $p = .0077$ )

$\therefore$  the beam is O.K. to stand the moment due to the horizontal force ( $BM = 572,400 \text{ in}^4$ )

As shown on preceding page steel must be placed in the tension and compression side of the beam (over the supports) because of the reversal of force due to the earth movements. But as there are 4-1 $\frac{1}{8}$ " bars at these points the beams will be of sufficient size + strength to carry the bending moment induced by horizontal forces.

B22

The beam would have the same R.M. = 1,260,000.

The steel is still more than necessary

BM caused by horizontal force = 572,000 in<sup>4</sup>

$\therefore$  B22 is of sufficient size + strength.

B21

Has same characteristics as B23 with regards to horizontal forces.



Strength of Original beam

$$M = \frac{19 \times 24.5 \times (125 + 150) \times 24.5}{30 \times 9.5} = 11000.$$

$$d = \sqrt{\frac{11000}{133.8}} = 9.1" \quad k = \frac{M}{bd^2}$$

$$a_s = \frac{11000 \times 12}{16000 \times 9.1 \times 8.5} = 1.08 \text{ in. per ft.}$$

use  $\frac{5}{8}$  @  $4\frac{1}{2}$ " or 21 bars over the 8 ft.

18 bars were used.

Size & strength required

$$B.M. = 106,000 \times 12 = 1,270,000 \text{ in}^{\#}$$

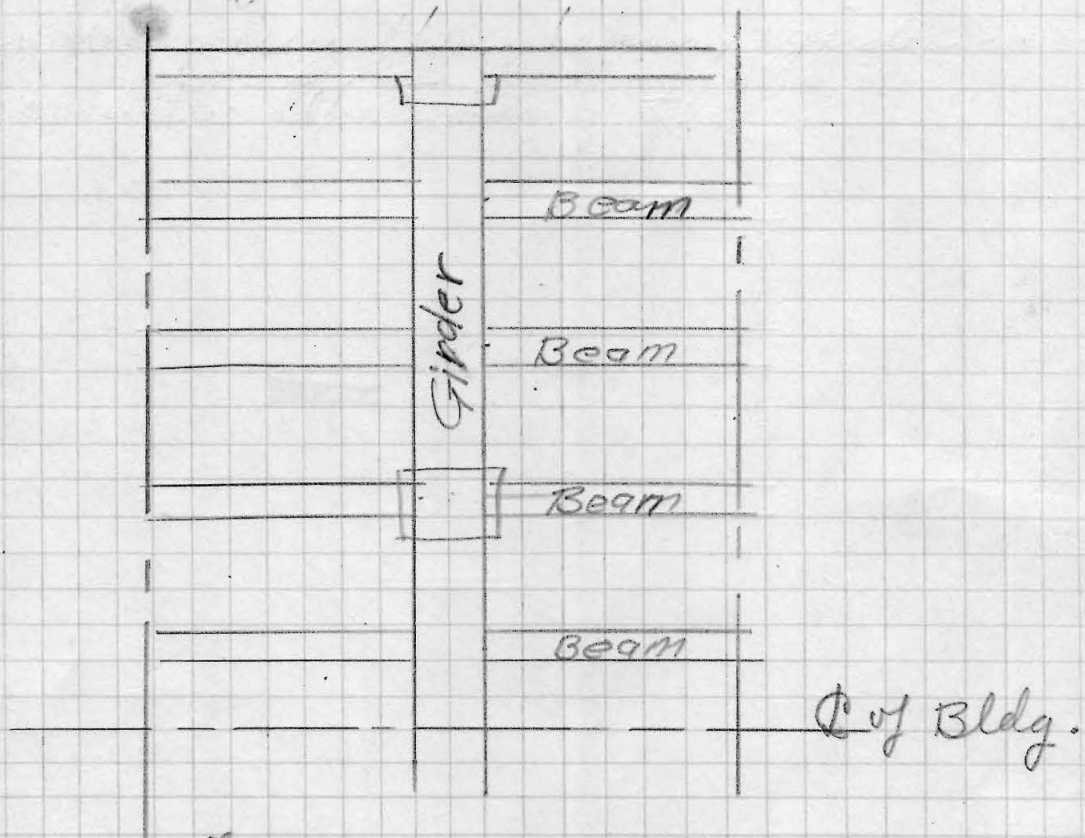
$$d = \sqrt{\frac{1,270,000}{133.8}} = \underline{\underline{28.2"}}$$

Such a depth as this would be out of the question.

It is necessary therefore to change the style of floor construction from flat slab construction to beam and girder construction.

# Beam & Girder design of floor system. 8th floor.

The beams will run parallel with the longest side of the building, with the girders across the building.



Assumptions -

Floor load all goes into beams.

Beam loads act as concentrated loads on girders.

Floor

$$D. Load = 50 \#$$

$$L. Load = 125 \#$$

$$\frac{175}{10}$$

$$BM = \frac{1 \times 175 \times 8 \times 8 \times 12}{10} = 13400 \text{ in} \#$$

$$d = \sqrt{\frac{13400}{133.8 \times 12}} = 2.9$$

use 4" slab.

$$a_s = \frac{13400}{16000 \times 3 \times .875} = .3 \sim 2 \text{ in per ft.}$$

$$\text{use } \frac{3}{8} \text{ in. } @ 5 \frac{1}{4} \text{ in.}$$

Beqm Calculate d for DL & LL.

$$\text{Load} = 175 \times 8 = 1550 / \text{ft}$$

$$\text{BM} = \frac{1}{10} \times 1500 \times 19 \times 19 \times 12 = 672000$$

at support

$$\begin{array}{r} \text{BM} \\ \text{RM} = 1074 \times 10 \times 17 \times 17 = 311000 \\ \hline 115 \overline{) 361000} \\ 240000 \end{array}$$

$$a_s = 0.677 \times 10 \times 17 = 1.31$$

$$a_s = \frac{24000}{16000} = \frac{1.50}{2.81} \quad T$$



$$C_1 = \frac{24000}{6670} = 3.60$$

$$\begin{array}{l} \frac{0.75}{660} = \frac{12.5}{x} \quad f_c = \frac{275}{375} \times 650 = 476 \\ f'_s = 476 \times (15 - 1) = 6670 \end{array}$$

Stirrups

$$V = 9.5 \times 1550 = 14700$$

$$v = \frac{14700}{11 \times 17 \times .875} = 10.5$$

$$\frac{W}{d} = \frac{1550}{14} = 97$$

$$\text{dist} = 5'9''$$

$$N_s \text{ of } \frac{3}{8} \text{ in. } = 5$$



## Center section

assuming "j" = .92

$$a_o = \frac{672000}{16000 \times .92 \times 16} = 2.87 \text{ sq in.}$$

∴ Steel in support would limit

## Girder

$$B.M. = 1550 \times 19 \times 8 \times 12 + \frac{400 \times 24 \times 24 \times 12}{10}$$

$$= 2,830,000 + 277,000$$

$$= 3,107,000$$

over support

$$B.M. =$$

$$R.M. = 133.8 \times 14 \times 30 \times 30$$

$$3,107,000$$

$$1690,000$$

$$30 \overline{) 1417000}$$

$$472,000$$

$$a_o' = 100977 \times 14 \times 30 = 4.07$$

$$a_o'' = \frac{472,000}{16000} = 2.95$$

$$a_o''' = 7.02 \text{ Tension}$$

$$f_c' = \frac{225}{375} \times 750 = 550.0$$

$$f_s' = 550 \times 14 = 7700.0$$

$$a_o'''' = \frac{472000}{7700} = 6.13 \text{ Comp.}$$

## Center

assuming j = .92

$$a_o = \frac{3107000}{16000 \times .92 \times 30} = 7.05 \text{ sq. in.}$$

Stamps

$$\sqrt{= 19 \times 1550 + 400 \times 12 = 39300}$$

$$30 \times 14 \times 120 = 5040$$

$$\frac{3}{8} \times \frac{3}{8} \times 2 \times 16000 = 4500$$

$$NS \frac{3}{8} = \frac{39300 - 5040}{4500} = 8$$

This floor would be typical of all the floors except the 10th + 12th + 2nd floors, that is:

Floor	Concrete 4"	Steel $\frac{3}{8}" @ 5\frac{1}{4}"$
Beams	10x19 outside	286 sq in
Girders	14x32 outside	705 sq in

This design would be all right without considering earthquake stresses. In considering earthquake stresses it would be necessary to change the girder on each floor.

Assume live load - not acting when horizontal force is acting on bldg.  
(100% assume not)

$$\begin{aligned}
 BM_{then} &= \frac{8}{10} \times \left( \frac{10 \times 19 \times 150}{144} \right) \times 19 \times 8 \times 12 + \frac{400 \times 24 \times 24 \times 12}{10} \\
 &= 2890000 + 270000 \\
 &= 559,000 \text{ in}^{\#}
 \end{aligned}$$

This value of BM should be added to BM caused by horizontal force.

# Size of Girders 8th floor

$$\begin{array}{rcl}
 \text{Earthquake BM} & = & 106000 \times 12 = 1,276000 \\
 \text{DL} & & \\
 \text{BM} & = & \begin{array}{r} 559000 \\ \hline 1,829000 \end{array} \\
 \text{RM} & = & 133.8 \times 12 \times 24 \times 11 = 925 \\
 & & \begin{array}{r} 21,6 = 1904000 \\ \hline 41800 \end{array}
 \end{array}$$

$$a'_b = 0.97 \times 12 \times 24 = 2.79$$

$$a''_b = \frac{41800}{16000} = \frac{2.61}{5.40} = T$$

$$f'_1 = 1100$$

$$C_{\infty} = \frac{41800}{7700} = 5.45 \text{ C}$$

7th

$$\begin{array}{rcl}
 M_E & = & 137 \times 12 = 1645000 \\
 \text{BM} & = & \begin{array}{r} 559000 \\ \hline 2204000 \end{array} \\
 \text{RM} & = & 133.8 \times 12 \times 26 \times 16 = 1085 \\
 & & \begin{array}{r} 23.4 \mid 1119000 \\ \hline 47800 \end{array}
 \end{array}$$

$$a'_b = 0.97 \times 12 \times 26 = 3.13$$

$$a''_b = \frac{47800}{16000} = \frac{2.99}{6.12} = T$$

$$C = \frac{47800}{7700} = 6.22 \text{ C}$$



6th floor

$$\begin{aligned}
 ME &= 176500 \times 12 = 2120000 \\
 BM &= 559 \\
 BM &= 26790.00 \\
 RM &= 133.8 \times 13 \times 28 \times 28 = 1365000 \\
 25.2 & \overline{) 1314000} \\
 & \quad 52200
 \end{aligned}$$

$$a'_b = 0097 \times 13 \times 28 = 3.53$$

$$a''_b = \frac{52200}{16000} = 3.26$$

$$a'''_b = 6.69 \quad T$$

$$C = \frac{52200}{7700} = 6.78 \quad C$$

5th floor

$$\begin{aligned}
 ME &= 215000 \times 12 = 2580000 \\
 BM &= 559 \\
 BM &= 31390.00 \\
 RM &= 133.8 \times 14 \times 29 \times 29 = 157500 \\
 26.1 & \overline{) 1564000} \\
 & \quad 59800
 \end{aligned}$$

$$a'_b = 0097 \times 14 \times 29 = 3.94$$

$$a''_b = \frac{59800}{16000} = 3.73$$

$$a'''_b = 7.67 \quad T$$

$$C = \frac{59800}{7700} = 7.76 \quad C$$

# 4th floor

32

$$MK = 254500 \times 12$$

$$= 3054000$$

$$BM =$$

$$= \frac{559000}{3609000}$$

$$RM = 133.8 \times 15 \times 32 \times 30$$

$$= 1810$$

$$27 \quad \frac{11799000}{66600}$$

$$a^I = 0097 \times 15 \times 30 = 4.36$$

$$a^{II} = \frac{66600}{16000} = 4.16$$

$$a^{III} = 8.52 \quad T$$

$$C = \frac{66600}{7700} = 8.65 \quad C$$

# 3rd floor

$$MK = 294000 \times 12$$

$$= 3528000$$

$$BM =$$

$$= \frac{559}{4189000}$$

$$RM = 133.8 \times 15 \times 32 \times 32$$

$$= 205$$

$$28.8 \quad \frac{12038000}{71700}$$

$$a^I = 5097 \times 15 \times 32 = 4.65$$

$$a^{II} = \frac{66600}{16000} = 4.16$$

$$a^{III} = 9.13 \quad T$$

$$C = \frac{71700}{7700} = 9.31 \quad C$$

2nd floor

$$M_E = 347200 \times 12 = 4170000$$

BM

$$RM = 133.6 \times 16 \times 33 \times 33 = 233$$

$$29.7 \overline{) 2394000} \\ \underline{80500}$$

$$a'_s = 0.097 \times 16 \times 33 = 5.28$$

$$a''_s = \frac{80500}{16000} = 5.03$$

$$a'''_s = \frac{5.03}{10.31} \quad \checkmark$$

$$C = \frac{80500}{7700} = 10.45 \quad C$$

1st floor

$$M_E = 403000 \times 12 = 4840000$$

BM

$$RM = 133.8 \times 16 \times 35 \times 35 = 262$$

$$31.5 \overline{) 2775000} \\ \underline{88200}$$

$$a'_s = 0.097 \times 16 \times 35 = 5.43$$

$$a''_s = \frac{88200}{16000} = 5.52$$

$$a'''_s = \frac{5.52}{10.95} \quad \checkmark$$

$$C = \frac{88200}{7700} = 11.45 \quad C$$



Floor	Concrete (outside)	T	Steel C
8	12 x 26	5.40	5.45
7	12 x 28	6.12	6.22
6	13 x 30	6.84	6.78
5	14 x 31	7.67	7.76
4	15 x 32	8.52	8.65
3	15 x 34	9.13	9.31
2	16 x 35	10.31	10.45
1	16 x 37	10.95	11.45

The stirrups required would be approximately the same as before, that is 8 or 9 -  $3/8$ "

The increase in shear due to the increase in size of girder would be neutralized by the increased shear that the large beam would be able to carry

The shear at the center of the columns is the greatest and the shear at the interior columns is twice as much as that on the wall columns.

As the columns are (with hooping) they would be strong enough to stand the shear.

There is a possibility that the present longitudinal steel will also stand the bending moment caused by the earthquake stresses.

The condition that must be met that the column would be less likely to with stand is the direct stress that comes on the column.

The results of these direct stresses will be investigated first.

The method followed in finding the direct stresses gave values for all columns but the direct stresses on the interior columns were neutralized because of the difference in direction of stress.

# Direct Stresses. (Col 7)

8th Floor

$$\begin{array}{r} \text{DL} = 39200 \\ \text{direct stress} = \frac{39}{43100} \end{array}$$

assume 3.0% steel.

$$P = f_c A [1 + (n-1)p]$$

$$A = \frac{P}{f_c [1 + (n-1)p]}$$

$$f_c [1 + (n-1)p] = 800 [1 + (5-1)0.30] = 1136$$

$$A = \frac{43100}{1136}$$

$$A = 37.9 \text{ sq in}$$

$$\text{Present Col} = 12 \times 12 = 144$$

OK

7th Floor

$$\begin{array}{r} \text{DL} = 1211 \\ \text{DS} = \frac{127}{133800} \end{array}$$

$$A = \frac{133800}{1136} = 117.8 \text{ sq in}$$

$$\text{Present Col} = \frac{14 \times 14}{4} = 196 \quad \text{OK}$$

6th Floor

$$\begin{array}{r} \text{DL} = 2015 \\ \text{DS} = \frac{240}{2255} \end{array}$$

$$A = \frac{225500}{1136} = 198 \text{ sq in}$$

$$\text{Present Col} = \frac{\pi \times 18 \times 18}{4} = 254 \quad \text{OK}$$



5th floor

31

$$\begin{aligned} DL &= 2801 \\ DS &= \frac{3840}{318500} \end{aligned}$$

$$A = \frac{318000}{1136} = 280 \text{ sq in}$$

$$\text{Present Col} = \frac{\pi \times 20^2 \times 20}{4} = 314$$

OK

4th floor

$$\begin{aligned} DL &= 3610 \\ DS &= \frac{562}{4172} \end{aligned}$$

$$A = \frac{36100}{1136} = 367 \text{ sq in}$$

$$\text{Present Col} = \frac{\pi \times 22^2 \times 22}{4} = \underline{\underline{380}}$$

3rd floor

$$\begin{aligned} DL &= 4462 \\ DS &= \frac{772}{5174} \end{aligned}$$

$$A = \frac{517400}{1136} = 455 \text{ sq in}$$

$$\text{Present Col} = \frac{\pi \times 24^2 \times 24}{4} = \underline{\underline{453}} \text{ OK}$$

## 2nd floor

58

$$DL = 5181$$

$$DS = \frac{101600}{619100}$$

$$A = \frac{619100}{1136} = 536 \text{ sq in}$$

$$\text{Present Col} = \frac{\pi \times 26 \times 26}{4} = 531 \text{ Neg}$$

## 1st floor

$$DL = 5946$$

$$DS = \frac{1396}{7342}$$

$$A = \frac{7342}{1136} = 646 \text{ sq in}$$

$$\text{Present Col} = \frac{\pi \times 27 \times 27}{4} = 573 \text{ Neg.}$$

$$\text{increase to 29} = \frac{\pi \times 29 \times 29}{4} = 661 \text{ OK}$$

## Basement

$$DL = 6254$$

$$DS = \frac{1627}{8381}$$

$$A = \frac{838100}{1136} = 739 \text{ sq in}$$

$$\text{Present Col} = \frac{\pi \times 29 \times 29}{4} = 661 \text{ NG}$$

$$\text{increase to 31} = \frac{\pi \times 31 \times 31}{4} = 755 \text{ sq in OK}$$

### Bending Moments.

All columns are square, that is, the core is circular with two inches of concrete outside of each end of a diameter. This makes the side of the square column four inches greater than the core diameter.

In calculating for the necessary steel " $d$ " will be taken as equal to the core diameter plus two inches, " $b$ " equal to the side of the column.

Taking into account a reversal of direction of force, it is necessary to have the same amount of steel on opposite side of the column.

The bending moment is twice as much on the interior columns as it is on the wall columns, so those will be checked first.



Bending Moments (Art 18)

8th floor

$$M_s = p s j b d^2$$

$$p = \frac{.3906}{16 \times 14} = .00174$$

$$k = \sqrt{2 \times .00174 \times 15 + (.00174 \times 15)^2} = .00174 \times 15$$

$$k = 0.202$$

$$j = .923$$

$$b = 16$$

$$d = 14$$

$$M_s = .00174 \times 16.000 \times .923 \times 16 \times 14 \times 14$$

$$= 80,600$$

$$BM \text{ on Col} = 95,600 \times 12 = 1,148,000$$

∴ steel must be added.

337,000

$$BM =$$

$$RM = 133.816 \times 14 \times 14$$

$$1,148,000$$

$$420$$

$$12.6 \times 728,000$$

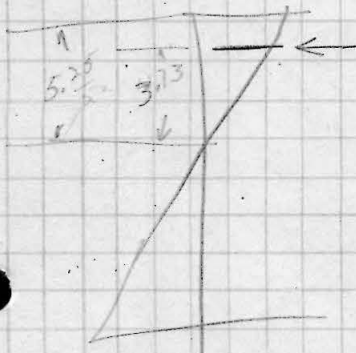
$$578,000$$

229

$$d_s = 16 \times 14 \times 0.077 = 2.17$$

$$d_s = \frac{60,750}{16,000} = 3.61$$

$$d_s = \frac{578,000}{T} = 5.78$$



$$k = \frac{3}{4}$$

$$\frac{4.73}{5.25} \times 750 = 550$$

$$f_s = 550 \times (15 - 1) = 7700$$

$$\text{Comp St. } \frac{578,000}{7700} = 7.50 \text{ in } \phi$$

use 7.50 on each side to take care of reversal action.

# 7th floor

41

$$BM = 12 \times 117.5 = 1,410,000$$

$$RM = 133.8 \times 20 \times 18 \times 18 = \frac{866}{16.2} \overline{) 5440.00}$$

$$34000$$

$$a'_s = .18 \times 20 \times .0097 = 3.49$$

$$a'' = \frac{34000}{16000} = \frac{21.2}{5.61} \quad T$$

$$\frac{34000}{7700} = 4.41 \quad C$$

# 6th floor

$$BM = 12 \times 1566 = 1880000$$

$$RM = 133.8 \times 24 \times 22 \times 22 = \frac{1552}{19.8} \overline{) 329000}$$

$$16600$$

$$a'_s = 22 \times 24 \times .0097 = 5.12$$

$$a'' = \frac{16600}{16000} = \frac{10.4}{6.16} \quad T$$

$$C = \frac{16600}{7700} = 2.16$$

# 5th floor

$$BM = 12 \times 196.8 = 2350000$$

$$RM = 133.8 \times 27 \times 25 \times 25 = \frac{226}{22.5} \overline{) 90000}$$

$$4000$$

$$a'_s = 27 \times 25 \times .97 = 6.55$$

$$a'' = \frac{4000}{16000} = \frac{25}{6.80} \quad T$$

C is negligible.

## 4th floor

$$BM = 12 \times 230 = 2820000$$

$$RM = 133.8 \times 28 \times 26 = \frac{253}{234 \overline{) 290000} \\ 12400}$$

$$a'_s = 28 \times 26 \times 0.097 = 7.28$$

$$a''_s = \frac{12400}{16000} = \frac{7.8}{16000}$$

$$a'''_s = 8.06$$

## 3rd floor

$$BM = 12 \times 274 = 3,290,000$$

$$RM = 133.8 \times 30 \times 28 \times 26 = \frac{3140}{25.7 \overline{) 150,000} \\ 5950}$$

$$a'_s = 30 \times 28 \times 0.097 = 8.15$$

$$a''_s = \frac{5950}{16000} = \frac{3.7}{16000}$$

$$a'''_s = 8.52$$

## 2nd floor

$$BM = 12 \times 313 = 3760000$$

$$RM = 133.8 \times 32 \times 30 \times 30 = \frac{3850000}{90000 \text{ over}}$$

$$a'_s = 30 \times 32 \times 0.097 = 9.30$$

## 1st floor

$$BM = 12 \times 382.8 = 4590000$$

$$RM = 133.8 \times 34 \times 32 \times 32 = \frac{4520000}{28.8 \overline{) 70000} \\ 2430}$$

$$a'_s = 34 \times 32 \times 0.097 = 10.52$$

$$a''_s = \frac{2430}{16000} = \frac{1.5}{16000}$$

$$a'''_s = 10.67$$



# Basement

143

$$BM = 12 \times 425 = 5,100,000$$

$$PM = 133.8 \times 34 \times 32 \times 32 = 452$$

$$28.8 \overline{) 590,000} \\ \underline{20500}$$

$$a_0 = 34 \times 32 \times 0.097 = 10.52$$

$$a'_0 = \frac{20500}{16000} = 1.28$$

$$a''_0 = 12.80$$

## Wall Column # 1

$$BM = 12 \times 47800 = 575000$$

$$PM = 133.8 \times 16 \times 14 \times 14 = 420000$$

$$12.6 \overline{) 55000} \\ \underline{12300}$$

$$a'_0 = 0.097 \times 14 \times 16 = 2.12$$

$$a''_0 = \frac{12300}{16000} = 1.72$$

$$a'''_0 = 2.94$$

T

$$Conf. = \frac{28200}{7700} = 3.66 \text{ C}$$

## 7th floor

$$BM = 12 \times 58750 = 705000$$

$$PM = 133.8 \times 18 \times 16 \times 16 = 616000$$

$$14.4 \overline{) 89000} \\ \underline{6170}$$

$$a'_0 = 0.097 \times 18 \times 16 = 2.77$$

$$a''_0 = \frac{6170}{16000} = 3.9$$

$$a'''_0 = 3.68$$

6th floor

44

$$\begin{aligned} BM &= 78300 \times 12 = 940000 \\ RM &= 1070 \times 22 \times 20 \times 20 = 940000 \end{aligned}$$

$$a_0 = 0.077 \times 20 \times 22 = 3.39$$

5th floor

$$\begin{aligned} BM &= 98400 \times 12 = 1180000 \\ RM &= 102 \times 24 \times 22 \times 22 = 1180000 \end{aligned}$$

$$a_0 = 0.073 \times 24 \times 22 = 3.85$$

4th floor

$$\begin{aligned} BM &= 117500 \times 12 = 1410000 \\ RM &= 1945 \times 26 \times 24 \times 24 = 1410000 \end{aligned}$$

$$a_0 = 0.067 \times 24 \times 26 = 4.18$$

3rd floor

$$\begin{aligned} BM &= 137000 \times 12 = 1645000 \\ RM &= 188 \times 28 \times 26 \times 26 = 1645000 \end{aligned}$$

$$a_0 = 0.063 \times 26 \times 28 = 4.58$$

2nd floor

$$\begin{aligned} BM &= 156500 \times 12 = 1880000 \\ RM &= 80.0 \times 30 \times 28 \times 28 = 1880000 \end{aligned}$$

$$a_0 = 0.056 \times 30 \times 28 = 4.76$$

1st floor

$$\begin{aligned} BM &= 191400 \times 12 = 2300000 \\ RM &= 88.1 \times 31 \times 29 \times 29 = 2300000 \end{aligned}$$

$$a_0 = 0.063 \times 29 \times 31 = 5.65$$

# Basement

45

$$BM = 212,500 \times 12 = 2,550,000$$

$$RM = 80.5 \times 33 \times 31 \times 31 = \frac{255}{\text{---}}$$

$$as = 0057 \times 31 \times 33 = 5.84$$

The ratio of the steel in the N+S sides of Col#7 to the steel in the E+W sides will be approximately the same ratio as in Col#8. See pages 40-43 & 57-58

The ratio of N+S steel to E+W steel in Col#8 is about 1/2, the same may be applied to Col#7



Force North & South

48

Considering Columns 11 to 21

Dead Load Roof

$$LL = \left( \frac{24.5 + 24}{2} \right) 170 \times 30 = 123800$$

$$DL = 36.0 + 35.2 + 90.0 + 92.2 + 197.7 + 263.6 + 205.7 + 61.2 + 92.2 + 83.6 - 123.8 = \underline{1023.6}$$

8th floor

$$LL = \left( \frac{24.5 + 24}{2} \right) \times 170 \times 1.25 = 515000 + 123.8 = 6388$$

$$DL = 94.7 + 89.5 + 203.2 + 208.7 + 308.2 + 374.1 + 321.2 + 176.7 + 207.7 + 115.5 + 157.2 - 6388 = \underline{1597.9}$$

7th floor

$$LL = 515000 \times 2 = 330000 + 123.8 = 11538$$

$$DL = 152.8 + 143.1 + 312.0 + 318.7 + 414.4 + 480.3 + 432.7 + 289.7 + 320.7 + 226.5 + 239.7 - 11538 = \underline{22558}$$

6th floor

$$LL = 515 \times 3 + 123.8 = 1668.8$$

$$DL = 210.3 + 196.3 + 416.0 + 425.2 + 516.4 + 582.3 + 538.7 + 394.2 + 425.2 + 390.9 + 319.9 - 1668.8 = \underline{2696.6}$$

5th floor

$$LL = 515 \times 4 + 123.8 = 2183.8$$

$$DL = 266.6 + 248.4 + 520.2 + 531.8 + 618.5 + 684.8 + 645.3 + 564.7 + 531.9 + 451.2 + 397.4 - 2183.8 = \underline{3217.0}$$

4th floor

$$LL = 515 \times 5 + 123.8 = 2698.8$$

$$DL = 324.0 + 305.6 + 625.9 + 639.0 + 721.8 + 787.4 + 752.8 + 611.9 + 640.0 + 559.4 + 480.0 - 2698.8 = \underline{3749.6}$$

3rd floor

$$LL = 515 \times 6 + 123.8 = 3213.8$$

$$DL = 381.0 + 359.3 + 731.9 + 747.7 + 826.5 + 892.1 + 961.5 + 718.0 + 745.2 + 664.8 + 560.0 - 3213.8 = \underline{4294.2}$$

## 2nd floor

$$LH = 515 \times 7 + 123.8 = 3728.8$$

$$DL = 442.0 + 415.4 + 810.9 + 805.0 + 881.5 + 947.0 + 941.5 + 825.3 + 851.5 + 769.6 + 641.3 - 3728.8 = \underline{\underline{4702.2}}$$

## 1st floor

$$LH = 515 \times 8 + 123.8 = 4243.8$$

$$DL = 515.7 + 485.8 + 919.9 + 915.7 + 988.5 + 1051.3 + 1050.5 + 935.3 + 961.5 + 878.8 + 712.4 - 4243.8 = \underline{\underline{5201.6}}$$

Weight of individual floor in 1000#

Roof	1023.6 - 0	=	1023.6
8th	1599.7 - 1023.6	=	474.3
7th	2255.8 - 1599.7	=	657.9
6th	2696.6 - 2255.8	=	440.8
5th	3217.0 - 2696.6	=	520.4
4th	3749.6 - 3217.0	=	522.6
3rd	4274.2 - 3749.6	=	524.6
2nd	4702.2 - 4274.2	=	428.0
1st	5201.6 - 4702.2	=	509.4
			8   4078.0
			509.7

This means 50000# at each floor and 100000 at the roof ( $\frac{1}{10}$  of Dead Weight)  
 Our attention will be taken mainly to the effects on Column #18; important results that affect the other members will be noted, however.





## Direct Stresses

It was shown in the other solution that there were two stresses of an equal and opposite nature being applied to all interior columns so the resultant would be zero

### Beams



$$F \text{ at } A = 38.35$$

$$F \text{ at } B = 27.25$$

$$F \text{ greatest at } C = 95$$



$$F \text{ at } A = 58.3 - 38.3 = 20$$

$$F \text{ at } B = 41.6 - 27.2 = 14.4$$

$$F \text{ greatest at } C = 46.7$$

These stresses will be the same for all the remaining floors

The direct stresses vary inversely as the distance from the load.

# B.M. in Beams

It was found that the B.M. in each beam on the individual floors was the same.  
This being the case we will take the simplest

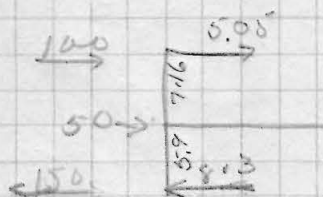
Case

100 →



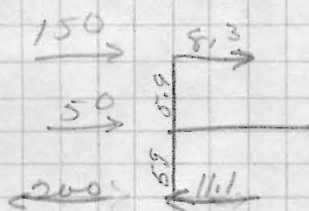
$$M = 5.05 \times 71.6 = 362^{\#}$$

8th floor



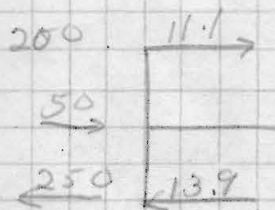
$$M = 5.05 \times 71.6 + 8.13 \times 59 = 85.2$$

7th floor



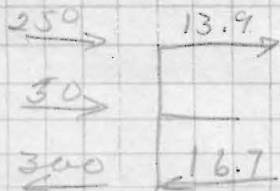
$$M = (81.3 + 111.1) 5.9 = 114.5$$

6th floor



$$M = (111.1 + 131.9) 5.9 = 147.5$$

5th floor



$$M = (131.9 + 161.7) 5.9 = 180.5$$

4th floor

<u>300</u> →	16.7 →
<u>50</u> →	
<u>350</u>	<u>19.5</u>

$$M = (16.7 + 19.5) 5.9 = 213.5$$

3rd floor

<u>350</u> →	19.5 →
<u>40</u> →	
<u>400</u>	<u>22.3</u>

$$M = (19.5 + 22.3) 5.9 = 246.8$$

2nd floor

<u>400</u> →	22.3 →
<u>50</u> →	
<u>450</u>	<u>25.1</u>

$$M = (22.3 + 25.1) 5.9 = 279.0$$

1st floor

<u>450</u> →	25.1 →
<u>50</u> →	
<u>500</u>	<u>27.9</u>

$$M = (25.1 + 27.9) 5.9 = 312.2$$



The B.M. on interior columns is twice as much as on the wall columns and will be alone considered.

Floor	expression	B M
Roof	$11.1 \times 7.6$	79.5
8	$16.6 \times 5.9$	98.1
7	$22.2 \times 5.9$	131.0
6	$27.8 \times 5.9$	164.0
5	$33.4 \times 5.9$	197.0
4	$39.0 \times 5.9$	240.0
3	$44.6 \times 5.9$	263.0
2	$50.2 \times 5.9$	296.0
1	$55.8 \times 5.9$	329.0

# Beams Design.

$$BM = 36.2 \times 12 = 432000$$

$$RM = 133.8 \times 12 \times 20 \times 20 = 642000$$

DL BM is negligible

$$a_s = 0.097 \times 12 \times 20 = 233$$

present steel = 1.56

∴ increase to 233

8th floor

$$BM = 85.2 \times 12 = 1020000$$

$$RM = 133.8 \times 11 \times 19 \times 19 = 528000$$

$$17.1 \overline{) 292000} \\ \underline{128800}$$

$$a_s = 0.097 \times 11 \times 19 = 2.03$$

$$a_s = \frac{25800}{16000} = 1.80$$

$$3.83$$

$$\frac{28800}{7700} = 3.75 \quad \text{C}$$

7th floor

$$BM = 12 \times 1145 = 1375000$$

$$RM = 133.8 \times 12 \times 21 \times 21 = 709000$$

$$19.9 \overline{) 666000} \\ \underline{33200}$$

$$a_s = 12 \times 21 \times 0.097 = 2.44$$

$$a_s = \frac{33200}{16000} = 2.07$$

$$a_s = 4.51 \quad \text{T}$$

$$C = \frac{33200}{7700} = 4.31$$

6th floor

$$BM = 12 \times 147.5 = 1770000$$

$$RM = 133.8 \times 13 \times 22.5 \times 22.5 = \frac{880000}{2025} = 43900$$

$$a'_b = 13 \times 22.5 \times 0.097 = 2.83$$

$$a''_b = \frac{43900}{16000} = 2.74$$

$$a''_b = 5.57 \text{ T}$$

$$C = \frac{43900}{7700} = \underline{\underline{5.70 \text{ C}}}$$

5th floor

$$BM = 12 \times 180.5 = 2165000$$

$$RM = 133.8 \times 13 \times 25 \times 25 = \frac{1085}{225} = 48200$$

$$a'_b = 13 \times 25 \times 0.097 = 3.13$$

$$a''_b = \frac{48200}{16000} = 3.01$$

$$a''_b = 5.83 \text{ T}$$

$$C = \frac{48200}{7700} = \underline{\underline{5.61 \text{ C}}}$$

4th floor

$$BM = 12 \times 213.5 = 2560000$$

$$RM = 133.8 \times 14 \times 26.5 \times 26.5 = \frac{1314}{23.85} = 55200$$

$$a'_b = 14 \times 26.5 \times 0.097 = 3.60$$

$$a''_b = \frac{55200}{16000} = 3.45$$

$$a''_b = 6.86 \text{ T}$$

$$C = \frac{55200}{7700} = \underline{\underline{6.77 \text{ C}}}$$



53

2nd floor

$$BM = 12 \times 246.8 = 2950000$$

$$RM = 133.8 \times 14 \times 28 \times 28 = \frac{1470000}{25.2}$$

$$\frac{1470000}{25.2} = 548000$$

$$a_b = 14 \times 28 \times 0.097 = 3.80$$

$$a_b = \frac{548000}{16000} = 3.42$$

$$a_b = 7.20 \checkmark$$

$$C = \frac{54800}{7700} = 7.13 \text{ @}$$

2nd floor

$$BM = 12 \times 279 = 3350000$$

$$RM = 133.8 \times 14 \times 30 \times 30 = \frac{1685000}{27}$$

$$\frac{1685000}{27} = 616000$$

$$a_b = 14 \times 30 \times 0.097 = 4.08$$

$$a_b = \frac{616000}{16000} = 38.5$$

$$a_b = 7.93 \checkmark$$

$$C = \frac{61600}{7700} = 8.00 \text{ @}$$

1st floor

$$BM = 12 \times 312.2 = 3750000$$

$$RM = 133.8 \times 15 \times 31 \times 31 = \frac{1930000}{27.9}$$

$$\frac{1930000}{27.9} = 653000$$

$$a_b = 15 \times 31 \times 0.097 = 4.52$$

$$a_b = \frac{653000}{16000} = 41.8$$

$$a_b = 8.70 \checkmark$$

$$C = \frac{65300}{7700} = 8.47 \text{ @}$$

No change will be made in the columns to stand the direct stress, for the force can only act either north and south or east and west.

It will be necessary however to add steel on the north and south sides of the columns however to stand the Bending moment.

8th floor

$$BM = 12 \times 79.5 = 955000$$

$$RM = 133.8 \times 16 \times 14 \times 14 = 2120000$$

$$12.6 \overline{) 1535000} \\ \underline{42500}$$

$$a'_s = 16 \times 14 \times 0.0097 = 217$$

$$a'_b = \frac{42500}{16000} = 2.65$$

$$a''_b = \frac{217}{4.82} = T$$

$$C = \frac{42500}{7700} = 5.52 \quad \textcircled{C}$$

7th floor

$$BM = 12 \times 98.1 = 1178000$$

$$RM = 133.8 \times 20 \times 18 \times 18 = 8670000$$

$$16.2 \overline{) 3110000} \\ \underline{19200}$$

$$a'_s = 20 \times 18 \times 0.0097 = 3.49$$

$$a'_b = \frac{19200}{16000} = 1.20$$

$$a''_b = \frac{3.49}{4.69} = T$$

$$C = \frac{19200}{7700} = 2.49 \quad \textcircled{C}$$

6th floor

$$BM = 12 \times 131 = 1570000$$

$$RM = 133.8 \times 24 \times 22 \times 22 = 155$$

$$19.8 \overline{) 20000} \\ \underline{1010}$$

$$a'_s = 24 \times 22 \times 0.0097 = 5.12$$

$$a''_b = \frac{1010}{16000} = 0.06$$

$$a'''_b = 5.18$$



3rd floor

$$BM = 12 \times 164 = 1970000$$

$$RM = 116.5 \times 27 \times 25 \times 25 = 197$$

$$a_s = 27 \times 25 \times 0.081 = 5.46$$

4th floor

$$BM = 12 \times 197 = 237$$

$$RM = 125 \times 28 \times 26 \times 26 = 237$$

$$a_s = 28 \times 26 \times 0.090 = 6.54$$

3rd floor

$$BM = 12 \times 240 = 2880000$$

$$RM = 122.5 \times 30 \times 28 \times 28 = 288$$

$$a_s = 28 \times 30 \times 0.088 = 7.80$$

2nd floor

$$BM = 12 \times 263 = 3160000$$

$$RM = 109.6 \times 32 \times 30 \times 30 = 3160000$$

$$a_s = 32 \times 30 \times 0.079 = 7.58$$

1st floor

$$BM = 12 \times 296 = 3570000$$

$$RM = 102.5 \times 34 \times 32 \times 32 = 3570000$$

$$a_s = 32 \times 34 \times 0.073 = 7.94$$

Basement

$$BM = 12 \times 329 = 3950000$$

$$RM = 113.5 \times 34 \times 32 \times 32 = 3950000$$

$$a_s = 34 \times 32 \times 0.081 = 8.80$$

Amount of steel that is necessary to be added to col. 18 (E & W BM)

8th floor.

Col. 18 has a square core on 8th floor with  $4 \times \frac{5}{8}$  bars. one of these bars on each side which can be included in the steel needed.

$$\text{Steel needed} = 7.50 \quad \text{area of } \frac{5}{8} \text{ rod} = .39$$

$$\therefore \text{add } 7.09 \text{ sq in.}$$

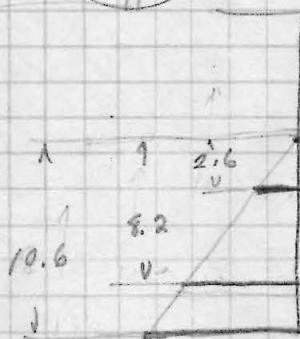
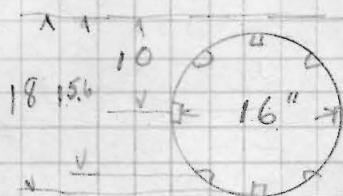
7th floor

5 -  $\frac{3}{4}$  bars.

$$\rho = .0097$$

$$k = 410$$

$$41 \times 18 = 7.4$$



$$3900 \times 2 \times .56 = 4360$$

$$12400 \times 2 \times .56 = 13900$$

$$16000 \times 1 \times .56 = 8960$$

$$\underline{27210 \#}$$

amt steel required at 18" for BM = 561

$$561 \times 16000 = 89600$$

$$\text{amt supplied} = 27210$$

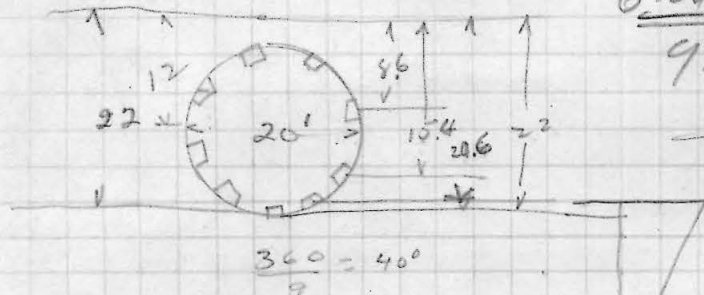
$$\frac{89600 - 27210}{16000} = \underline{\underline{3.90}} \text{ amt to be added.}$$

6th floor

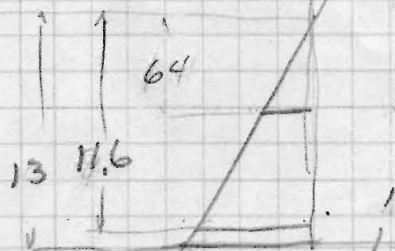
9-7/8" bars.

p = 0097 k = 41

41 x 22 = 9"



$$\frac{360}{9} = 400$$



$$7880 \times 2 \times .765 = 12000$$

$$14300 \times 2 \times .765 = 21900$$

$$16000 \times 1 \times .765 = 12100$$

$$46000$$

amt steel need at 16000 = 6.16

$$6.16 \times 16000 = 98600$$

$$46000$$

$$52600 = 3.29$$

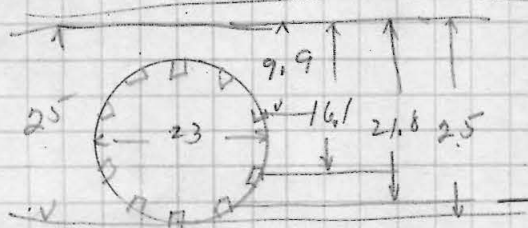
$$16000$$

5th floor

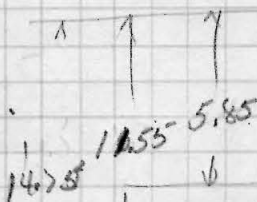
16-1" bars.

p = 0097 k = 41

25 x 41 = 10.25



$$\frac{360}{10} = 36$$



$$6350 \times 2 \times 1 = 12700$$

$$12500 \times 2 \times 1 = 25000$$

$$16000 \times 1 \times 1 = 16000$$

$$53700$$

amt steel need at 16000 = 6.80

$$6.80 \times 16000 = 108700$$

$$53700$$

$$55000 = 3.44$$

$$16000$$



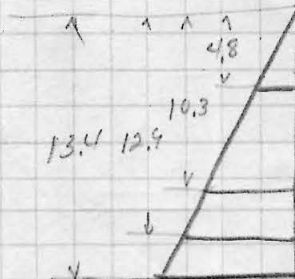
# 2nd floor

13-1" bars.

$$p = 0.097 \quad k = .41$$

$$.41 \times 26 = 10.65$$

$$\frac{360}{13} = 27.50$$



$$4300 \times 2 \times 1 = 8600$$

$$9240 \times 2 \times 1 = 18480$$

$$15400 \times 2 \times 1 = 30800$$

$$16000 \times 1 \times 1 = 16000$$

$$\frac{73880}{16000} = 4.62$$

$$\text{ant of steel @ 16000} = 8.06$$

$$8.06 \times 16000 = 129$$

$$\frac{73880}{16000} = 4.62$$

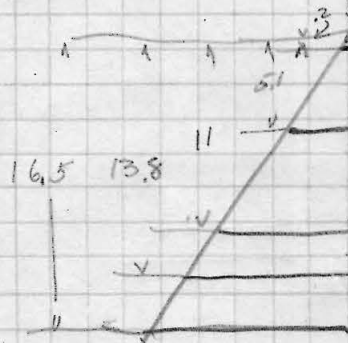
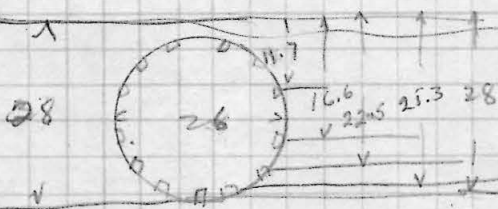
$$\frac{55120}{16000} = 3.45$$

# 3rd floor

$$p = 0.097$$

$$k = .41$$

$$.41 \times 28 = 11.5$$



$$194 \times 2 \times 11.25 = 4400$$

$$4780 \times 2 \times 11.25 = 10750$$

$$10650 \times 2 \times 11.25 = 24000$$

$$13400 \times 2 \times 11.25 = 30200$$

$$16000 \times 1 \times 11.25 = 18000$$

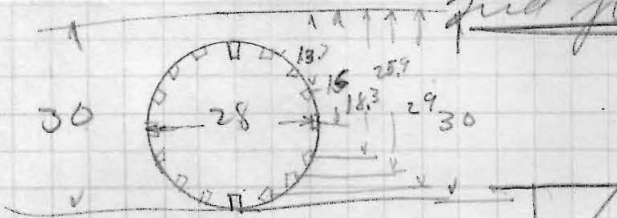
$$\frac{83150}{16000} = 5.19$$

$$\text{ant steel @ 16000} = 8.52$$

$$8.52 \times 16000 = 136000$$

$$\frac{83150}{16000} = 5.19$$

$$\frac{52850}{16000} = 3.30$$



16-1 7/8"

$p = 0.097$   $K = 41$

$41 \times 30 = 1230$

$\frac{360}{16} = 22.5$



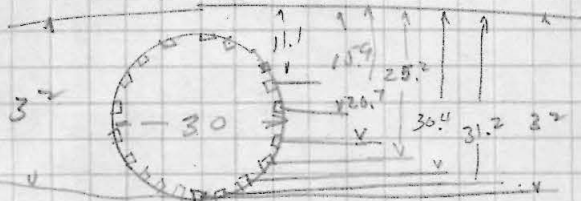
$220 \times 2 \times 1/25 =$	1600
$8300 \times 2 \times 1/25 =$	18700
$12300 \times 2 \times 1/25 =$	25400
$15100 \times 2 \times 1/25 =$	34000
$16000 \times 1 \times 1/25 =$	18000
	<u>97700</u>

amt steel needed @ 16000 = 930

$930 \times 16000 = 1490000$

$\frac{97700}{5130.0} = 32.0$

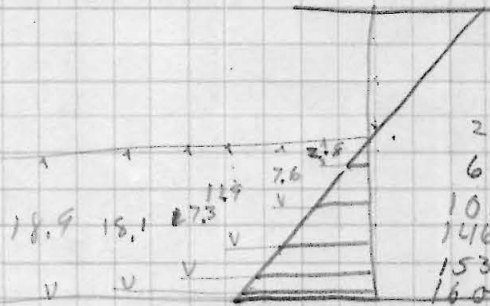
1st floor 19-1 1/8"



$p = 0.097$   $K = 10041$

$041 \times 32 = 13.1$

$\frac{360}{19} = 18.95$



$2400 \times 2 \times 1/25 =$	5400
$6450 \times 2 \times 1/25 =$	14500
$10100 \times 2 \times 1/25 =$	22700
$14600 \times 2 \times 1/25 =$	32800
$153000 \times 2 \times 1/25 =$	34400
$16000 \times 1 \times 1/25 =$	18000
	<u>127800</u>

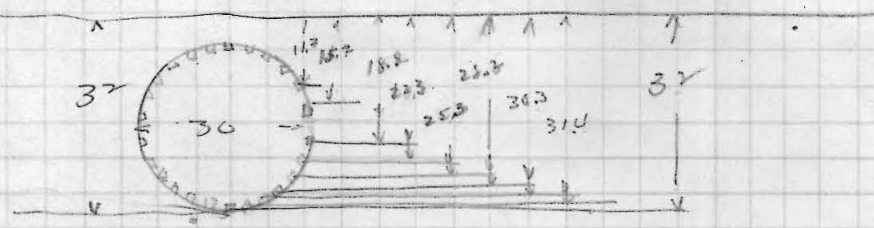
steel needed @ 16000 = 10.67

$10.67 \times 16000 = 170500$

$\frac{127800}{43700} = 2.73$

Basement

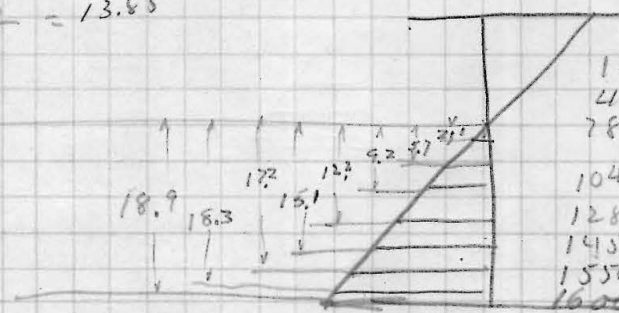
26-1/8 bar



$p=0.097 \quad k=41$

$0.41 \times 32 = 13.1$

$\frac{360}{26} = 13.85$



12800	x 2 x 11/25	4000
4800	x 2 x 11/25	10800
7800	x 2 x 11/25	17500
10400	x 2 x 11/25	23400
12800	x 2 x 11/25	28800
14300	x 2 x 11/25	32600
15500	x 2 x 11/25	34900
16000	x 1 x 11/25	18000
		<u>170000</u>

steel needed for 16000 = 12.80

$12.80 \times 16000 = 205000$

$\frac{170000}{35000} = \underline{\underline{2.19}}$



Steel that must be added to slant  
N+S B.M.

8th floor

Col. 11 has a square core on the 8th floor with  
4- $\frac{5}{8}$ " sq rods, one on each side which can  
be included in the steel needed.

$$\begin{aligned}\text{Steel needed} &= 5.52'' \\ \text{area of } 4 \times \frac{5}{8}'' &= .39 \\ \text{amt to be added} &= 5.13''\end{aligned}$$

7th floor.

amt steel needed at 16000 #/in = 4.69

$$\begin{aligned}16000 \times 4.69 &= 75100 \\ \text{Stress taken by original Col} &= \frac{27210}{47890} = 2.99'' \text{ to be added} \\ &\frac{16000}\end{aligned}$$

6th floor

$$\begin{aligned}\text{steel @ } 16000 &= 5.18 \\ 16000 \times 5.18 &= 83000 \\ \text{stress taken by original col} &= \frac{46000}{37000} = 2.31 \text{ to be added} \\ &\frac{16000}\end{aligned}$$

5th floor

$$\begin{aligned}\text{steel @ } 16000 &= 5.46 \\ 16000 \times 5.46 &= 90300 \\ \text{stress taken by original Col} &= \frac{53700}{36600} = 2.29 \text{ to be added} \\ &\frac{16000}\end{aligned}$$

4th floor

$$\begin{aligned}\text{steel @ } 16000 &= 6.54 \\ 16000 \times 6.54 &= 104500 \\ \text{stress taken by original Col} &= \frac{73880}{30620} = 1.92 \text{ to be added} \\ &\frac{16000}\end{aligned}$$

## 3rd floor

$$\text{steel @ 16000} = 7.80$$

$$16000 \times 7.80 = 124800$$

$$\text{stress taken by orig. col} = \frac{83150}{41650} = 2160 \text{ to be added}$$

## 2nd floor

$$\text{steel @ 16000} = 7.58$$

$$16000 \times 7.58 = 121500$$

$$\text{stress taken by orig. col} = \frac{97700}{23800} = 1491 \text{ to be added}$$

## 1st floor

$$\text{steel @ 16000} = 7.94$$

$$16000 \times 7.94 = 127000$$

$$\text{stress taken by orig. col} = \underline{127800}$$

none needed.

## basement.

$$\text{steel @ 16000} = 8.80$$

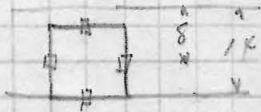
$$16000 \times 8.80 = 158000$$

$$\text{stress taken by orig. col} = \underline{170000}$$

none needed.

Amount of steel to be added to Col 7 (E-W B.M.)

8th floor



4 - 5 bars  
 $P = 0.0097$   $k = .41$   
 $.41 \times 14 = 5.7$

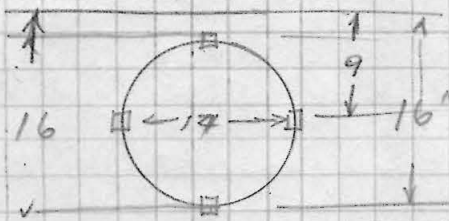
2.3  
 8.3  
 $2280 \times 2 \times .39 = 1780$   
 $16000 \times 1 \times .39 = \frac{6240}{8020}$

steel @ 16000 = 294  
 $16000 \times 2.94 = 47040$   
 stress taken by orig col =  $\frac{8020}{38990} \sim 244$  to be added  
 $\frac{16000}{16000}$

7th floor

4 - 3 bars

$P = 0.0097$   $k = .41$   
 $.41 \times 16 = 6.5$



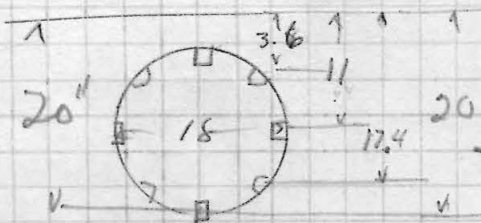
9  
 16  
 9.5  
 $2500 \times 2 \times .56 = 2800$   
 $16000 \times 1 \times .56 = \frac{9000}{11800}$

steel @ 16000 = 3.08  
 $16000 \times 3.08 = 49280$   
 stress taken by orig col =  $\frac{11800}{36500} \sim 228$  to be added  
 $\frac{16000}{16000}$



6th floor.

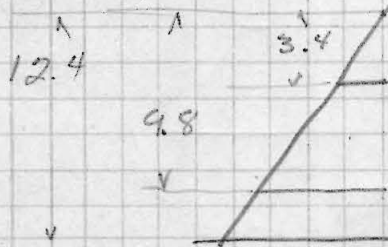
8 -  $\frac{5}{8}$  bars



$$p = .0077$$

$$k = .38$$

$$20 \times .38 = 7.6$$



$$4400 \times 2 \times .39 = 3400$$

$$12600 \times 2 \times .39 = 9800$$

$$16000 \times 1 \times .39 = 6200$$

$$19400$$

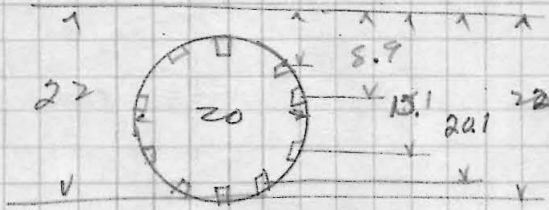
$$\text{steel @ } 16000 = 3.39$$

$$16000 \times 3.39 = 54200$$

$$\text{stress taken by air coil} = 1.9400$$

$$\frac{34800 - 2.17 \text{ to be added}}{16000}$$

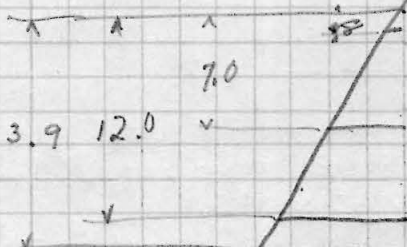
5th floor



$$p = .0073$$

$$k = .37$$

$$.37 \times 22 = 8.1$$



$$9600 \times 2 \times .56 = 10000$$

$$8050 \times 2 \times .56 = 9000$$

$$13800 \times 2 \times .56 = 15500$$

$$16000 \times 1 \times .56 = 8950$$

$$34450$$

$$\text{steel @ } 16000 = 3.85$$

$$16000 \times 3.85 = 61600$$

$$\text{stress taken by air coil} = 3.4450$$

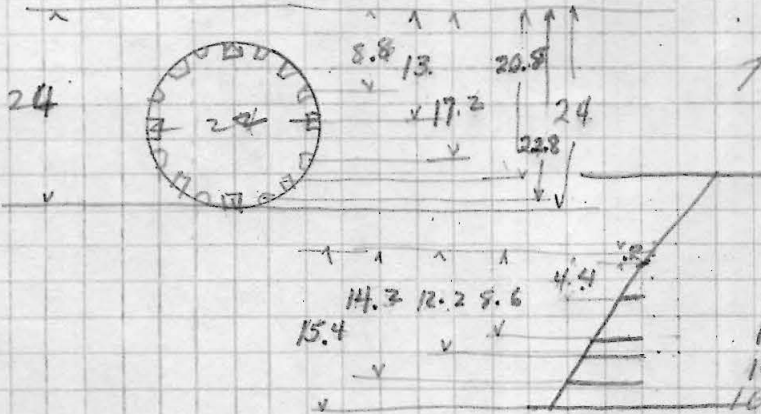
$$\frac{27150}{16000} = 1.70 \text{ to be added}$$

# 4th floor

12 -  $\frac{7}{8}$  bars

$$p = .0667 \quad k = .36$$

$$.36 \times 24 = 8.6$$



200	x 2	x .76	=	300
4500	x 2	x .76	=	6800
9000	x 2	x .76	=	13700
12700	x 2	x .76	=	19000
14700	x 2	x .76	=	22000
16000	x 1	x .76	=	12000
				<u>73800</u>

steel @ 16000 = 4.18

$$16000 \times 4.18 = 67000$$

steel taken by orig col = 73800

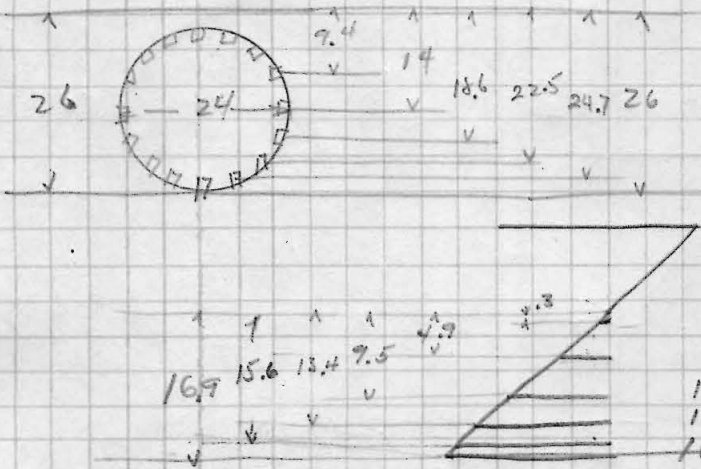
none needed.

# 3rd floor

12 - 1" bars

$$p = .063 \quad k = .35$$

$$.35 \times 26 = 9.1$$



300	x 2	x 1	=	600
4600	x 2	x 1	=	9200
9000	x 2	x 1	=	18000
12700	x 2	x 1	=	25400
14700	x 2	x 1	=	29400
16000	x 1	x 1	=	16000
				<u>98600</u>

steel @ 16000 = 4.58

$$16000 \times 4.58 = 73500$$

steel taken by orig col = 98600

none needed.

Amount of steel to be added to col 7 (N+S B<sub>y</sub>)

As the Bart. in col 7 were not calculated for N+S forces, the amount of steel to be added will be taken in the same proportion that steel was needed for E+W forces in col. 18 and 7.

8th floor

$$\frac{5.13}{7.09} \times 2.44 = 1.77 \text{ to be added.}$$

7th floor

$$\frac{2.99}{5.61} \times 2.28 = 1.21 \text{ to be added.}$$

6th floor

$$\frac{2.31}{3.29} \times 2.17 = 1.57 \text{ to be added.}$$

5th floor

$$\frac{2.29}{3.44} \times 1.70 = 1.13 \text{ to be added.}$$

none needed from 4th floor to basement



# Steel in orig. Columns.

Col 7

Col 18

$$8th \quad 1.56 \times 16.75 \times 12 = 312$$

$$1.56 \times 14 \times 12 = 262$$

$$7th \quad 2.25 \times 13.33 \times 12 = 360$$

$$4.15 \times 13.25 \times 12 = 715$$

$$6th \quad 3.12 \times 13.33 \times 12 = 503$$

$$6.89 \times 13.33 \times 12 = 1103$$

$$5th \quad 5.62 \times 13.33 \times 12 = 900$$

$$10.1 \times 13.58 \times 12 = 1628$$

$$4th \quad 9.19 \times 13.33 \times 12 = 1470$$

$$13 \times 13.62 \times 12 = 2124$$

$$3rd \quad 12 \times 13.62 \times 12 = 1960$$

$$16.45 \times 14.08 \times 12 = 2775$$

$$2nd \quad 14 \times 13.62 \times 12 = 2290$$

$$20.25 \times 14.08 \times 12 = 3415$$

$$1st \quad 17.1 \times 14.62 \times 12 = 3980$$

$$24.05 \times 15.08 \times 12 = 4350$$

$$base \quad 21.57 \times 15.15 \times 12 = 4000$$

$$32.90 \times 15.75 \times 12 = 6220$$

15773 cuin

22592 cuin

## Steel in new columns.

Col 7

Col 7

$$8th \quad 312 + 2(2.44 + 1.17) 16.75 \times 12 = 2002$$

$$7th \quad 360 + 2(2.28 + 1.21) 13.33 \times 12 = 1470$$

$$6th \quad 503 + 2(2.17 + 1.57) 6.67 \times 12 = 1030$$

$$5th \quad 900 + 2(1.70 + 1.13) 6.67 \times 12 = 1353$$

$$4th \quad 1470 + 2(1.45 + 1.09) 13.62 \times 12 = 1960$$

$$3rd \quad 1960 + 2(1.30 + 1.00) 12 \times 12 = 2290$$

$$2nd \quad 2290 + 2(1.49) 14 \times 13.62 \times 12 = 3980$$

$$1st \quad 3980 + 2(1.62) 17.1 \times 14.62 \times 12 = 4000$$

$$base \quad 4000$$

19655 cuin

# Core 18

8th	$262 + 2(7.09 + 5.13)14 \times 12$	=	4875
7th	$715 + 2(3.80 + 2.99)13.25 \times 12$	=	2905
6th	$1103 + 2(3.29 + 2.31)6.67 \times 12$	=	1998
5th	$1628 + 2(3.44 + 2.29)6.79 \times 12$	=	2623
4th	$2124 + 2(3.45 + 1.92)6.81 \times 12$	=	3000
3rd	$2775 + 2(3.30 + 2.60)7.04 \times 12$	=	3771
2nd	$3415 + 2(3.20 + 1.49)7.04 \times 12$	=	4208
1st	$4350 + 2(2.73 + 0)7.54 \times 12$	=	4843
Base	$6220 + 2(2.19 + 0)15.75 \times 12 \times 1.25$	=	7255
			<hr/> 34978 cuin

Comparison of Old & New Design  
Slabs

Roof.

The roof slab is the same for both cases

4" slab steel -  $\frac{3}{8}$ "  $\phi$  @ 7" +  $\frac{3}{8}$ " @ 18"

$$\text{Vol conc.} = .33 \times 18.87 \times 36.48 = 223 \text{ cu ft.}$$

$$\text{Vol steel} = .3 \times 36.48 \times 18.87 \times 12 = 2475 \text{ cu in.}$$

8th floor - 1st floor

Old.

$$\text{Vol. Conc.} = .66 \times 18.87 \times 36.48 + 6.33 \times 8 \times 3.15 + 6.33 \times 4 \times 3.15$$

$$= 443 + 29$$

$$= 472 \text{ cu ft.}$$

$$\text{Vol steel (N+S)} = (\overset{G}{27.3} \times 14 \times 12) + (\overset{H}{4.35} \times 14 \times 12) 2.5 + (\overset{5}{2.75} \times 14 \times 12) 2.75 +$$

$$(\overset{T}{1.87} \times 14 \times 12) = 3658 \text{ cu in.}$$

$$E+W = (2.75 \times 30.6 \times 12) 2 + (2.25 \times 30 \times 12) 1.5$$

$$= 3234 \text{ cu in.}$$

$$\text{Vol. conc.} = 472 \text{ cu ft.}$$

$$\text{Vol steel} = 6892 \text{ cu in.}$$

New.

$$\text{Vol. conc.} = .33 \times 18.87 \times 36.48 = 223 \text{ cu ft.}$$

$$\text{Vol steel} = .32 \times 19 \times 36.5 \times 12 = 3660 \text{ cu in.}$$



# Inside Beams (8th-1st)

No beams on old design.

New,

inside beams.

$$\text{Vol concrete} = \frac{10 \times (18-4) 19}{12} \times 3 = 55.4 \text{ cu ft.}$$

$$\text{Vol steel} = \frac{3.72 \times 19 \times 15 \times 12 \times 3}{12} = 3820 \text{ cu in.}$$

## Roof.

Roof same in both cases.

$$\text{Vol con.} = \frac{12 \times (20-4) 19}{12} \times 3 = 76.0 \text{ cu ft.}$$

$$\begin{aligned} \text{Vol steel} &= 2 \left[ \frac{(78+76) 19 \times 15 \times 12}{144} \right] + 1 \left[ \frac{(78+1) 19 \times 15 \times 12}{144} \right] \\ &= 1054 + 609 = 1663 \text{ cu in.} \end{aligned}$$

## Col. Beams.

### Roof

Old

$$\text{Vol con.} = \frac{12 \times (20-4) 19}{12} \times 1 = 25.3 \text{ cu ft.}$$

$$\text{Vol steel} = \frac{(78+76) 19 \times 15 \times 12}{144} = 527 \text{ cu in.}$$

New

$$\text{Vol con.} = \frac{12 \times (20-4) 19}{144} = 25.3 \text{ cu ft.}$$

$$\text{Vol steel} = 2.33 \times (9 \times 15 \times 12) = 792 \text{ cu in.}$$

8 ft.

Old. no beams.

New

$$\text{Vol con} = \frac{11 \times 17 \times 19}{144} = 24.7 \text{ cu ft.}$$

$$\text{Vol steel} = 3.83 \times 342 \times 1.75 = 2290 \text{ cu in.}$$

new

7th floor

$$\text{Vol con} = \frac{12 \times 19 \times 19}{144} = 30.1 \text{ cu ft}$$

$$\text{Vol steel} = 3.42 \times 4.5 \times 1.75 = 2700 \text{ cu in.}$$

new

6th floor

$$\text{Vol con} = \frac{13 \times 20.5 \times 19}{144} = 35.2 \text{ cu ft}$$

$$\text{Vol steel} = 5.70 \times 3.42 \times 1.75 = 3420 \text{ cu in.}$$

5th floor

new

$$\text{Vol con} = 13 \times 23 \times \frac{19}{144} = 39.5 \text{ cu ft}$$

$$\text{Vol steel} = 5.83 \times 3.42 \times 1.75 = 3490 \text{ cu in.}$$

4th floor

new

$$\text{Vol con} = 14 \times 24.5 \times \frac{19}{144} = 45.2 \text{ cu ft}$$

$$\text{Vol steel} = 6.86 \times 3.42 \times 1.75 = 4120 \text{ cu in.}$$

3rd floor

new

$$\text{Vol con} = 14 \times 26 \times \frac{19}{144} = 48.1 \text{ cu ft}$$

$$\text{Vol steel} = 7.20 \times 3.42 \times 1.75 = 4310 \text{ cu in.}$$

2nd floor

new

$$\text{Vol con} = 14 \times 28 \times \frac{19}{144} = 57.8 \text{ cu ft}$$

$$\text{Vol steel} = 8.00 \times 3.42 \times 1.75 = 4836 \text{ cu in.}$$

new 1st floor

$$\text{Vol con} = 15 \times 29 \times \frac{19}{144} = 57.4 \text{ cu ft}$$

$$\text{Vol steel} = 870 \times 342 \times 1.75 = 5200 \text{ cu in}$$


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## Girders Roof

old:

$$\text{Vol con} = 12 \times 26 \times \frac{36.5}{144} - \frac{12 \times 16 \times 12 \times 3}{1728} = 25.7 \text{ cu ft}$$

$$\text{Vol steel} = 506 \times 42 \times 12 = 2550 \text{ cu in}$$

new

$$\text{Vol con} = 75.1 \text{ cu ft}$$

$$\text{Vol steel} = 2550 \times 2 = 5100 \text{ cu in}$$

## 5th floor

No old

new

$$\text{Vol con} = 12 \times 26 \times \frac{36.5}{144} - \frac{16 \times 14 \times 14 \times 3}{1728} - \frac{11 \times 17 \times 14}{1728} = 75.2 \text{ cu ft}$$

$$\text{Vol steel} = 849 \times 504 \times 1.75 = 7500 \text{ cu in}$$

new

## 7th floor

$$\text{Vol con} = 12 \times 28 \times \frac{36.5}{144} - \frac{10 \times 14 \times 15 \times 3}{1728} - \frac{11 \times 17 \times 15}{1728} = 82.9 \text{ cu ft}$$

$$\text{Vol steel} = 918 \times 504 \times 1.75 = 8100 \text{ cu in}$$

new

## 6th floor

$$\text{Vol con} = 13 \times 30 \times 2.53 - 15 \times 243 - 15 \times 108 = 193.2 \text{ cu ft}$$

$$\text{Vol steel} = 985 \times 504 \times 1.75 = 8800 \text{ cu in}$$

new

## 5th floor

$$\text{Vol con} = 14 \times 31 \times 2.53 - 16 \times 243 - 16 \times 108 = 184.3 \text{ cu ft}$$

$$\text{Vol steel} = 1064 \times 504 \times 1.75 = 9400 \text{ cu in}$$



new

4th floor

$$\text{Vol con} = 15 \times 34 \times 253 - 16 \times 243 - 16 \times 108 = 116.8 \text{ cuft}$$

$$\text{Vol steel} = 1085 \times 504 \times 1.25 = 9660 \text{ cuin}$$

new

3rd floor

$$\text{Vol con} = 15 \times 34 \times 253 - 16 \times 243 - 16 \times 108 = 123.3 \text{ cuft}$$

$$\text{Vol steel} = 1152 \times 504 \times 1.25 = 10160 \text{ cuin}$$

2nd floor

new

$$\text{Vol con} = 16 \times 35 \times 253 - 17 \times 243 - 17 \times 108 = 132.0 \text{ cuft}$$

$$\text{Vol steel} = 12.28 \times 504 \times 1.25 = 10800 \text{ cuin}$$

1st floor

new

$$\text{Vol con} = 16 \times 37.5 \times 253 - 17 \times 243 - 17 \times 108 = 146 \text{ cuft}$$

$$\text{Vol steel} = 12.90 \times 504 \times 1.25 = 11380 \text{ cuin}$$

Vol of old & New Concrete in Interior Col. 18

$$8th\ floor = \frac{16 \times 16 \times 11.75}{144} = 20.9$$

$$7th = \frac{20 \times 20 \times 11.75}{144} = 32.7$$

$$6th = \frac{24 \times 24 \times 11.75}{144} = 46.9$$

$$5th = \frac{27 \times 27 \times 11.75}{144} = 58.5$$

$$4th = \frac{28 \times 28 \times 11.75}{144} = 63.9$$

$$3rd = \frac{30 \times 30 \times 11.75}{144} = 73.4$$

$$2nd = \frac{32 \times 32 \times 11.75}{144} = 83.5$$

$$1st = \frac{34 \times 34 \times 11.75}{144} = 94.0$$

$$basement = \frac{34 \times 34 \times 11.75}{144} = 94.0$$

Vol of Old Concrete curb

$$8th = 16 \times 16 \times \frac{11.75}{144} = 20.9$$

$$7th = 18 \times 18 \times \frac{11.75}{144} = 26.4$$

$$6th = 22 \times 22 \times \frac{11.75}{144} = 34.4$$

$$5th = 24 \times 24 \times \frac{11.75}{144} = 46.8$$

$$4th = 26 \times 26 \times \frac{11.75}{144} = 55.0$$

$$3rd = 28 \times 28 \times \frac{11.75}{144} = 63.8$$

$$2nd = 30 \times 30 \times \frac{11.75}{144} = 73.4$$

$$1st = 31 \times 31 \times \frac{11.75}{144} = 78.2$$

$$basement = 33 \times 33 \times \frac{11.75}{144} = 89.0$$

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# Total Concrete

	Old		New
Floors {	roof 223 = 223		roof-1st = $223 \times 9 = 2007$
	8th-1st $472 \times 8 = 3776$		
	399.9 cu ft		2007 cu ft

Interior {	Roof 76	7.6 "	roof 76.5
Beams {	none		8th-1st = $8 \times 55.4$
			443.2
			<u>519.2</u>

Column {	Roof	25.3	25.3
	8th	none	24.7
	7th	"	30.1
	6th	"	35.2
Beams {	5th	"	39.5
	4th	"	45.2
	3rd	"	48.1
	2nd	"	51.6
	1st	"	57.4
		<u>257.3</u>	<u>357.3</u>

Girders {	Roof	75.1	75.1
	8th	none	75.2
	7th	"	82.9
	6th	"	93.2
	5th	"	104.3
	4th	"	116.8
	3rd	"	123.8
	2nd	"	137.0
	1st	"	146.0
		<u>75.1</u>	<u>954.3</u>

Old

New

Col. 18	8th	20.9
	7th	32.7
	6th	46.9
	5th	58.5
	4th	63.9
	3rd	73.4
	2nd	83.5
	1st	94.0
	bas	94.0
		<u>567.8</u>

20.9
32.7
46.9
58.5
63.9
73.4
83.5
94.0
94.0
<u>567.8</u>

Col 7	8th	20.9
	7th	26.4
	6th	39.6
	5th	46.8
	4th	55.0
	3rd	63.8
	2nd	73.4
	1st	84.2
	bas	89.0
		<u>502.9</u>

20.9
26.4
39.6
46.8
55.0
63.8
73.4
84.4
101.5
<u>535.6</u>

Old

New

Floor	39.99.0
Interior Beams	76.0
Col Beams	25.3
Girders	75.1
Col 18	567.8
Col 7	502.9
	<u>5246.1</u>

2007.0
519.2
357.3
954.3
567.8
535.6
<u>4941.2</u>

5246.1 cu ft

4941.2 cu ft

# Total Steel

Old

New

Floors { Roof 2475 = 2475  
 8th-1st 8x 6892 = 55136  
 57611

2475  
 8x3860 = 29280  
31755

Interior Beams { roof 1663  
 8th-1st none  
1663

1663  
 8x3820 = 30560  
 32223

Cul Beams { roof 527  
 8th none  
 7th "  
 6th "  
 5th "  
 4th "  
 3rd "  
 2nd "  
 1st "  
527

797  
 2290  
 2700  
 3420  
 3490  
 4120  
 4310  
 4780  
5200  
 28107

Girders { roof 2550  
 8th none  
 7th "  
 6th "  
 5th "  
 4th "  
 3rd "  
 2nd "  
 1st "  
2550

5110  
 7500  
 8100  
 8800  
 9400  
 9600  
 10160  
 10860  
11380  
 80910



Old

New

Cul 18	8th	262
	7th	715
	6th	1103
	5th	1628
	4th	2124
	3rd	2775
	2nd	3415
	1st	4350
	base	6220
		<u>22592</u>

4375
2905
1998
2623
3000
3771
4208
4843
<u>7255</u>
34978

Cul 7	8th	312
	7th	360
	6th	503
	5th	900
	4th	1470
	3rd	1960
	2nd	2290
	1st	3980
	base	4000
		<u>15773</u>

2002
1470
1030
1353
1470
1960
2290
3980
4000
<u>19655</u>

Floors 57611

31755

Interior Beams 1663

32223

Cul Beams 527

228107

girders 2550

80910

Cul 18 22592

34978

Cul 7 15773

19655

100716

227628

# Comparison of Designs

Old		New
Volume Concrete	52461 cu.ft	49412 Cu.ft
" Steel	100,716 cu.in	227,628 cu.in.

New Design has 94.3 % of Concrete of Old  
" " " 226.0 % of Steel of Old.